## Learning <br> Outcomes

## Framework

## April 2004

Mathematics Grades Primary-6

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Department of Education

# Learning Outcomes Framework Mathematics <br> Grades Primary-6 

## Grade Primary

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.
By the end of grade 3, students will be expected to Students will be expected to

- construct and communicate number meanings, and explore and apply estimation strategies, with respect to whole numbers
- concretely explore common fractions and decimals in meaningful situations
- read and write whole numbers and demonstrate an understanding of place value (to four places)
- order whole numbers and represent them in multiple ways
- apply number theory concepts (e.g., place value pattern) in meaningful contexts with respect to whole numbers and commonly used fractions and decimals

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 3, students will be expected to
Students will be expected to

- demonstrate an understanding of the connection between relevant, concrete experiences and the mathematical language and symbolism of the four basic operations
- recognize and explain the relationships among the four basic operations
- create and model problem situations involving whole numbers, using one or more of the four basic operations
- demonstrate proficiency with addition and subtraction facts
- apply computational facts and strategies with respect to the four basic operations and model addition and subtraction in situations involving whole numbers

B1 count the results when small groups are combined
B2 count the results when small groups are separated
B3 determine how many more one group has than another

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

By the end of grade 3, students will be expected to

- recognize, describe, extend, and create patterns and sequences in a variety of mathematical and real-world contexts (e.g., geometric, numeric, and measurement)

Students will be expected to
C1 copy and extend patterns including those involving number, shape, size, and colour
C2 copy patterns based on measurement attributes
C3 create patterns
C4 represent the same pattern in multiple ways

- use patterns to solve problems
- represent mathematical patterns and relationships in informal ways, including via open sentences (e.g., statements with missing addends)

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 3, students will be expected to

- measure and understand basic concepts and attributes of length, capacity, mass, area, and time

Students will be expected to
D1 compare and order objects based on length, capacity, and mass
D2 sequence events
D3 sort items based on measurement attributes

- identify and use non-standard and standard units of measurement and appreciate their role in communications
- estimate and determine measurements in every-day problem situations and develop a sense of the relative size of units


## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 3, students will be expected to

- explore and experiment with geometric shapes and relationships (including the orientation and perspectives of objects)
- describe, model, draw, and classify 2- and 3-D figures and shapes
- investigate and predict the results of combining, subdividing, and transforming shapes
- relate geometric ideas to number and measurement ideas and recognize and apply geometric principles in real-world situations

Students will be expected to
E1 develop spatial sense, including position-in-space and the language associated with it
E2 develop spatial sense, including eye-motor co-ordination
E3 sort and build with 2-D and 3-D shapes
E4 pattern with 2-D and 3-D shapes
E5 recognize, name, describe, and compare 3-D shapes (including sphere, cylinder, cone, and cube) and 2D shapes (including square, triangle, circle, and rectangle)

E6 build 2-D shapes using structured materials
E7 subdivide and change shapes
E8 make transformations of figures and shapes

E9 recognize familiar shapes occurring in the environment

GCO F: Students will solve problems involving the collection, display, and analysis of data.

By the end of grade 3, students will be expected to

- collect, record, organize, and describe relevant data
- construct concrete and pictorial displays of relevant data
- read and interpret displays of relevant data
- generate questions, develop and modify predictions and implement plans with respect to data analysis

Students will be expected to
F1 collect and organize data about issues of personal interest

F2 form and interpret "people" graphs
F3 interpret and create real and picture graphs

GCO G: Students will represent and solve problems involving uncertainty.
By the end of grade 3, students will be expected to

- conduct informal investigations of chance and estimate probabilities with respect to games and other simple, everyday situations


## Grade 1

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.

## By the end of grade 3, students will be expected to

- construct and communicate number meanings, and explore and apply estimation strategies, with respect to whole numbers
- concretely explore common fractions and decimals in meaningful situations
- read and write whole numbers and demonstrate an understanding of place value (to four places)
- order whole numbers and represent them in multiple ways
- apply number theory concepts (e.g., place value pattern) in meaningful contexts with respect to whole numbers and commonly used fractions and decimals

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 3, students will be expected to

- demonstrate an understanding of the connection between relevant, concrete experiences and the mathematical language and symbolism of the four basic operations
- recognize and explain the relationships
among the four basic operations
- create and model problem situations involving whole numbers, using one or more of the four basic operations


## Students will be expected to

A1 compare two sets for size in a variety of ways
A2 create equivalent sets and sets that differ by small amounts
A3 count in a variety of ways
A4 sort sets based on number
A5 match quantities with numerals
A6 count beyond 10 in a variety of ways
A7 estimate amounts between 10 and 100
A8 demonstrate an understanding of simple fractional parts

A9 order numbers and use ordinal language
A10 explore the meaning of the numbers between 10 and 20
A11 model numbers grouped in tens and ones
A12 compare 2-digit numbers

Students will be expected to
B1 recognize that addition is used to represent the joining of two groups
B2 recognize that subtraction is used to represent separating situations

B3 recognize the relationship between addition and subtraction
B4 recognize that subtraction can be used to solve missing addend problems
B5 recognize how to use addition or subtraction to solve comparison problems

B6 move freely among representing an addition or subtraction situation with a picture, a model, or a number sentence

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- demonstrate proficiency with addition and subtraction facts
- apply computational facts and strategies with respect to the four basic operations and model addition and subtraction in situations involving whole numbers
- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

By the end of grade 3, students will be expected to

- recognize, describe, extend, and create patterns and sequences in a variety of mathematical and real-world contexts (e.g., geometric, numeric, and measurement)
- use patterns to solve problems
- represent mathematical patterns and relationships in informal ways, including via open sentences (e.g., statements with missing addends)

B7 use mental strategies to find sums to 18 and differences from 18 or less
B8 know simple addition facts from among those for which the total is 10 or less and know the corresponding subtraction facts

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement. (continued)

- identify and use non-standard and standard units of measurement and appreciate their role in communications
- estimate and determine measurements in every-day problem situations and develop a sense of the relative size of units

D3 identify and use non-standard units to estimate and measure length, capacity, time, mass, and area
D4 read hours on an analog clock

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 3, students will be expected to

- explore and experiment with geometric shapes and relationships (including the orientation and perspectives of objects)
- describe, model, draw, and classify 2- and 3D figures and shapes
- investigate and predict the results of combining, subdividing, and transforming shapes
- relate geometric ideas to number and measurement ideas and recognize and apply geometric principles in real-world situations


## Students will be expected to

E1 develop aspects of spatial sense, including visual memory
E2 develop aspects of spatial sense, including figure ground perception
E3 sort, build, and pattern with 2-D and 3-D shapes
E4 recognize and represent angles
E6 describe attributes of and sort and compare 2-D and 3-D shapes

E5 recognize, name, describe, and represent a variety of 2-D and 3-D shapes
E7 recognize 2-D figures in 3-D shapes
E8 build, divide, and change 2-D shapes
E9 recognize, name, describe, and represent slides and reflections of 2-D shapes

E10 recognize and identify 2-D and 3-D shapes in the environment
E11 cover figures and fill shapes with countable nonstandard units

## GCO F: Students will solve problems involving the collection, display, and analysis of data.

By the end of grade 3, students will be expected to Students will be expected to

- collect, record, organize, and describe relevant F1 collect and organize data data
- construct concrete and pictorial displays of relevant data
- read and interpret displays of relevant data
- generate questions, develop and modify predictions and implement plans with respect to data analysis

F2 interpret and create concrete and picture graphs
F3 interpret and create pictographs and symbolic graphs

F4 pose oral questions in relation to conducting surveys and/or interpreting data

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO G: Students will represent and solve problems involving uncertainty.
By the end of grade 3, students will be expected to Students will be expected to

- conduct informal investigations of chance and estimate probabilities with respect to games and other simple, everyday situations

G1 predict whether an event can never occur, must always occur, or simply might occur sometimes

## Grade 2

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.

## By the end of grade 3, students will be expected to

- construct and communicate number meanings, and explore and apply estimation strategies, with respect to whole numbers
- concretely explore common fractions and decimals in meaningful situations
- read and write whole numbers and demonstrate an understanding of place value (to four places)
- order whole numbers and represent them in multiple ways
- apply number theory concepts (e.g., place value pattern) in meaningful contexts with respect to whole numbers and commonly used fractions and decimals


## Students will be expected to

A1 order numbers and use ordinal language
A2 count in a variety of ways
A3 estimate the size of numbers to the nearest multiple of 10

A4 identify simple fractions using models

A5 describe numbers in a variety of ways
A6 demonstrate an understanding of base-10 groupings
A7 model numbers to three places
A8 compare and order numbers by size
A9 recognize, extend, and create simple place-value patterns

GCO B: Students will demonstrate number sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 3, students will be expected to

- demonstrate an understanding of the connection between relevant, concrete experiences and the mathematical language and symbolism of the four basic operations
- recognize and explain the relationships among the four basic operations
- create and model problem situations involving whole numbers, using one or more of the four basic operations
- demonstrate proficiency with addition and subtraction facts

Students will be expected to
B1 recognize that multiplication can be used to determine the total amount in groups of equal size
B2 recognize that division can mean determining how many groups of a fixed size are in a larger group or fair sharing

B3 demonstrate an understanding that addition can be used to solve subtraction problems and vice versa
B4 create word problems involving addition and subtraction

B5 develop and apply strategies to learn addition and subtraction facts
B6 recall addition facts involving two addends, each less than 10 , and the related subtraction facts

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate number sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- apply computational facts and strategies with respect to the four basic operations and model addition and subtraction in situations involving whole numbers
- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

B7 demonstrate an understanding of basic principles of addition
B8 add 3 single-digit numbers
B9 model and perform the addition of two 2-digit numbers, with and without regrouping
B10 model and perform the subtraction of two 2-digit numbers, with and without regrouping

B11 estimate the sum or difference of two 2-digit numbers

B12 use technology to solve problems involving sums or differences of larger numbers

GCO C: Students will explore, recognize, represent and apply patterns and relationships, both informally and formally.

By the end of grade 3, students will be expected to

- recognize, describe, extend, and create patterns and sequences in a variety of mathematical and real-world contexts (e.g., geometric, numeric, and measurement)
- use patterns to solve problems
- represent mathematical patterns and relationships in informal ways, including via open sentences (e.g., statements with missing addends)


## Students will be expected to

C1 compare and contrast patterns
C2 demonstrate an understanding that there are often many ways to continue a pattern, unless a pattern rule is provided

C3 identify and use patterns in an addition table
C4 identify and extend place-value patterns
C5 represent patterns using their own notation or symbolism
C6 solve simple open sentences involving addition and subtraction facts

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 3, students will be expected to

- measure and understand basic concepts and attributes of length, capacity, mass, area, and time

Students will be expected to
D1 identify procedures not involving units to be used to compare areas

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement. (continued)

- identify and use non-standard and standard units of measurement and appreciate their role in communications

D2 demonstrate a sense of how long 1 cm and 1 m are
D3 estimate and measure length in non-standard and standard units
D4 recognize and explain why standard units are used
D5 demonstrate a sense of how much 1 L is
D6 estimate and measure capacity in non-standard and standard units
D7 demonstrate a sense of how much 1 kg is
D8 estimate and measure mass using non-standard and standard units
D9 estimate and measure time using non-standard units
D10 read hours and half-hours on a clock
D11 explore properties of the calendar
D12 choose appropriate units with which to estimate and measure, and perform the measurements
D13 demonstrate an understanding that the size of the unit used affects the number describing the measurement
D14 demonstrate an understanding that 100 cm makes up 1 m

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

## By the end of grade 3, students will be expected to

- explore and experiment with geometric shapes and relationships (including the orientation and perspectives of objects)
- describe, model, draw, and classify 2- and 3D figures and shapes


## Students will be expected to

E1 develop aspects of spatial sense, including perceptual constancy, perception of spatial relationships, and visual discrimination
E2 recognize 3-D shapes from drawings and from alternative perspectives
E3 sort, build, and pattern with 2-D and 3-D shapes
E4 recognize, name, and represent parallel lines and right angles

E5 recognize, name, describe, and represent parallelograms
E6 recognize, name, describe, and represent triangular, square, and rectangular prisms and pyramids
E7 cut and assemble nets of cubes and triangular, square, and rectangular prisms and pyramids
E8 recognize surfaces and faces of 3-D shapes

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships. (continued)

- relate geometric ideas to number and measurement ideas and recognize and apply geometric principles in real-world situations

E12 recognize and identify reflective symmetry in the environment
E13 make the connection between reflective symmetry and one-half using squares, rectangles, and circles
E14 make the connection between even/odd numbers and rectangles

GCO F: Students will solve problems involving the collection, display, and analysis of data.

By the end of grade 3, students will be expected to

- collect, record, organize, and describe relevant data
- construct concrete and pictorial displays of relevant data
- read and interpret displays of relevant data
- generate questions, develop and modify predictions and implement plans with respect to data analysis

Students will be expected to
F1 conduct simple surveys and record data

F2 create and interpret pictographs and symbolic bar graphs

F3 develop and modify predictions with respect to data collected or presented to them

GCO G: Students will represent and solve problems involving uncertainty.

By the end of grade 3, students will be expected to

- conduct informal investigations of chance and estimate probabilities with respect to games and other simple, everyday situations

Students will be expected to
G1 demonstrate an understanding that some events are more likely than others
G2 demonstrate an understanding that probability predictions need not always come true

## Grade 3

## General Curriculum Outcomes

## Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.
By the end of grade 3, students will be expected to Students will be expected to

- construct and communicate number meanings, and explore and apply estimation strategies, with respect to whole numbers
- concretely explore common fractions and decimals in meaningful situations
- read and write whole numbers and demonstrate an understanding of place value (to four places)
- order whole numbers and represent them in multiple ways
- apply number theory concepts (e.g., place value pattern) in meaningful contexts with respect to whole numbers and commonly used fractions and decimals

A1 compare and order whole numbers to thousands
A2 estimate the size of numbers to the nearest ten or hundred

A3 use simple fractions to describe situations

A4 demonstrate an understanding of base-10 groupings (units, tens, hundreds, thousands)
A5 record, model, and interpret numbers up to and including the thousands

A6 read numbers in several ways

A7 extend the place-value system to model and record numbers involving tenths
A8 order and compare decimals to tenths

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 3, students will be expected to

- demonstrate an understanding of the connection between relevant, concrete experiences and the mathematical language and symbolism of the four basic operations
- recognize and explain the relationships among the four basic operations
- create and model problem situations involving whole numbers, using one or more of the four basic operations

Students will be expected to
B1 recognize several meanings for multiplication
B2 recognize several meanings for division

B3 recognize the relationship between multiplication and division

B4 solve and create problems involving addition and/or subtraction
B5 solve and create problems involving multiplication and division with small numbers

- demonstrate proficiency with addition and subtraction facts


## General Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- apply computational facts and strategies with respect to the four basic operations and model addition and subtraction in situations involving whole numbers
- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

B6 add and subtract with and without regrouping (up to and including three-digit numbers)
B7 recognize principles of multiplication and division
B8 relate multiplication and division facts
B9 continue to estimate in addition and subtraction situations
B10 begin to estimate in multiplication and division situations

B11 mentally add and subtract two-digit and one-digit numbers
B12 mentally add and subtract rounded numbers
B13 use technology to solve problems involving larger numbers

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

## By the end of grade 3, students will be expected to

- recognize, describe, extend, and create patterns and sequences in a variety of mathematical and real-world contexts (e.g., geometric, numeric, and measurement)
- use patterns to solve problems
- represent mathematical patterns and relationships in informal ways, including via open sentences (e.g., statements with missing addends)

Students will be expected to
C1 recognize the pattern implicit in the place-value system
C2 recognize and create geometric patterns

C3 use and recognize the patterns in a multiplication table

C4 record a repeated addition pattern using multiplicative notation
C5 recognize the meaning of open sentences of the forms:

$$
a \times b=
$$

$$
a \times \square=c
$$

$$
\square \times b=c
$$

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 3, students will be expected to Students will be expected to

- measure and understand basic concepts and attributes of length, capacity, mass, area, and time


## General Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with meas urement. (continued)

- identify and use non-standard and standard D1 estimate and measure length in metres, decimetres, units of measurement and appreciate their role in communications and centimetres
D2 estimate and measure capacity in millilitres and litres
D3 estimate and measure mass in grams and kilograms
D4 estimate and measure area in non-standard units and square centimetres
- estimate and determine measurements in every-day problem situations and develop a sense of the relative size of units

D5 solve problems involving kilometres
D6 use appropriate units for capacity and mass
D7 read digital and analog clocks to the nearest five minutes
D8 continue to solve a wide variety of measurement problems

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 3, students will be expected to

- explore and experiment with geometric shapes and relationships (including the orientation and perspectives of objects)
- describe, model, draw, and classify 2 - and 3-D figures and shapes
- investigate and predict the results of combining, subdividing, and transforming shapes
- relate geometric ideas to number and measurement ideas and recognize and apply geometric principles in real-world situations

Students will be expected to
E1 continue their development of spatial sense with emphasis on perceptual constancy
E2 recognize and represent angles that are less than/more than right angles
E3 recognize, name, describe, and represent congruent angles and congruent polygons

E4 recognize, name, describe, and represent kite, and some concave, convex, and regular polygons
E5 recognize, name, describe, and represent different prisms and pyramids
E6 cut and assemble net patterns for pentagonal and hexagonal prisms and pyramids
E7 build skeletons of various prisms and pyramids to focus on edges and vertices

E8 predict the results of combining triangles and/or quadrilaterals
E9 find the lines of reflective symmetry of polygons
E10 recognize, name, describe, and represent half and quarter turns of 2-D figures

E11 recognize and identify various polygons, prisms, and pyramids in real-world contexts
E12 make the connection for rectangles between the arrays of squares forming them and the describing of their dimensions

## General Curriculum Outcomes Specific Curriculum Outcomes

GCO F: Students will solve problems involving the collection, display, and analysis of data.
By the end of grade 3, students will be expected to Students will be expected to

- collect, record, organize, and describe

F1 select appropriate strategies for collecting, relevant data

- construct concrete and pictorial displays of relevant data

F2 interpret and create pictographs in which each symbol represents more than one item

- read and interpret displays of relevant data
- generate questions, develop and modify predictions and implement plans with respect to data analysis

F3 create bar graphs using simple scales

F4 implement plans with respect to the collection of data

GCO G: Students will represent and solve problems involving uncertainty.

## By the end of grade 3, students will be expected to

- conduct informal investigations of chance and estimate probabilities with respect to games and other simple, everyday situations


## Students will be expected to

G1 predict and record results in experiments using spinners, coins, dice, coloured cubes, and other simple equipment

## Grade 4

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number-theory concepts.
By the end of grade 6, students will be expected to Students will be expected to

- demonstrate an understanding of number A1 identify and model fractions and mixed numbers meanings with respect to whole numbers, A2 interpret and model decimal tenths and hundredths fractions, and decimals
- explore integers, ratios, and percents in common meaningful situations
- read and write whole numbers and decimals

A3 model and record numbers to 99999
and demonstrate an understanding of place value (to millions and to thousandths)

- order whole numbers, fractions, and decimals and represent them in multiple ways

A4 compare and order whole numbers
A5 compare and order fractions
A6 rename fractions with and without the use of models
A7 compare and order decimals with and without models

- apply number theory concepts (e.g., prime numbers, factors) in relevant situations with respect to whole numbers, fractions, and decimals

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 6, students will be expected to

- model problem situations involving whole numbers and decimals by selecting appropriate operations and procedures
- model problem situations involving the addition and subtraction of simple fractions

Students will be expected to
B1 add and subtract decimals involving tenths and hundredths, and whole numbers to five digits
B2 demonstrate an understanding of multiplication meanings and applications
B3 demonstrate an understanding of the various meanings of division
B4 multiply 2-and 3-digit numbers by single-digit numbers concretely, pictorially, and symbolically
B5 divide 2- and 3-digit whole numbers by a singledigit divisor

B6 use models informally to add simple fractions with common denominators

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- explore algebraic situations informally
- apply computational facts and procedures (algorithms) in a wide variety of problem situations involving whole numbers and decimals

B7 demonstrate an understanding of use of the open frame as a place holder for a digit on some occasions and for a number on other occasions
B8 relate multiplication and division facts, using principles of these operations
B9 demonstrate a knowledge of multiplication facts to $9 \times 9$
B10 demonstrate an understanding of various treatments of remainders in division situations
B11 solve and create word problems involving whole number computations
B12 solve and create word problems involving adding and subtracting decimals (to hundredths) justify the reasonableness of, results in relevant problem situations involving whole numbers and decimals

- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations
estimate sums and differences of whole numbers and decimals
B14 estimate the product or quotient of 2- or 3-digit numbers and single-digit numbers

B15 mentally solve appropriate addition and subtraction computations
B16 mentally multiply 2-digit numbers by 10 or 100
B17 use technology for computations involving many decimal places or large whole numbers

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

By the end of grade 6 , students will be expected to

- describe, extend, and create a wide variety of patterns and relationships to model and solve problems involving real-world situations and mathematical concepts
- explore how a change in one quality in a relationship affects another
- represent mathematical patterns and relationships in a variety of ways (including rules, tables, and one- and two-dimensional graphs)


## Students will be expected to

C1 demonstrate an understanding of the relationship between adding decimals and adding whole numbers
C2 apply the pattern identified when multiplying by increasing powers of ten
C3 use patterns to solve computation problems
C4 understand how a change in either $a$ or $b$ in $a+b$, $a-b, a \times b$, or $a \div b$ will affect the result of the computation
C5 represent multiplication facts either in a table or graphically
C6 complete open sentences of the form $a \times b=\square$, $a \mathrm{x} \square=c, a \div b=\square$, and $a \div \square=c$

- solve linear equations using informal, nonalgebraic methods


## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 6, students will be expected to Students will be expected to

- extend understanding of measurement concepts and attributes to include volume, temperature, perimeter, and angle

D1 recognize and demonstrate that objects of various shapes can have the same area
D2 recognize and demonstrate that objects of the same area can have different perimeters
D3 measure volume, using non-standard units
D4 estimate and determine the volume of rectangular prisms, using centimetre cubes
D5 recognize that the measure of an angle indicates an amount of turn
D6 estimate and measure angles, using non-standard units
D7 use a thermometer to read temperatures

- communicate using standard units, understand the relationship among commonly used SI units (e.g., mm, cm, m, km ) and select appropriate units in given situations
- estimate and apply measurement concepts and skills in relevant problem situations and select and use appropriate tools and units
- develop and apply rules and procedures for determining measures (using concrete and graphing models)

D8 estimate and measure in millimetres, centimetres, decimetres, metres, and kilometres
D9 estimate and measure area in square centimetres
D10 solve relevant problems involving millilitres and litres, grams and kilograms

D11 relate dimensions and areas of rectangles to factors and products

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 6, students will be expected to

- identify, draw, and build physical models of geometric figures
- solve problems using geometric relationships and spatial reasoning

Students will be expected to
E1 draw various nets for rectangular prisms and cubes
E2 construct models for various cylinders, cones, prisms, and pyramids
E3 construct shapes given isometric drawings
E4 explore relationships among 3-D shapes
E5 find all possible composite figures that can be made from a given set of figures

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

## GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships. (continued)

- describe, model, and compare 2- and 3-D figures and shapes, explore their properties, and classify them in alternate ways
- investigate and predict the results of transformations and begin to use them to compare shapes and explain geometric concepts (e.g., symmetry and similarity)

E6 recognize, name, describe, and construct acute and obtuse angles
E7 recognize, name, describe, and construct equilateral, isosceles, and scalene triangles
E8 make generalizations about the angle, side length, and parallel side properties of the various quadrilaterals
E9 sort quadrilaterals under property headings
E10 make generalizations about the number of vertices, edges, and faces of various prisms, pyramids, cones, and cylinders

E11 predict and confirm the results of various 2-D figures under slides, reflections, and quarter/half turns
E12 make generalizations about the reflective symmetry property of the various quadrilaterals

GCO F: Students will solve problems involving the collection, display, and analysis of data.
By the end of grade 6, students will be expected to Students will be expected to

- collect, organize, describe relevant data in multiple ways
- construct a variety of data displays (including tables, charts, and graphs) and consider their relative appropriateness
- read, interpret, and make and modify predictions from displays of relevant data
- develop and apply measures of central tendency (mean, median, and mode)
- formulate and solve simple problems (both real-world and from other academic disciplines) that involve the collection, display, and analysis of data and explain conclusions which may be drawn

F1 recognize and use a variety of methods for the collection and organization of data
F2 describe data maxima, minima, range, and frequency

F4 display position, using ordered pairs on a grid
F5 construct bar graphs, pictographs, and stem-andleaf plots

F3 read and interpret bar graphs, line graphs, pictographs, and stem-and-leaf plots
F6 interpolate data from a display
F7 describe data, using the mean

F8 explore real-world issues of interest to students and for which data collection is necessary to determine an answer

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO G: Students will represent and solve problems involving uncertainty.
By the end of grade 6, students will be expected to Students will be expected to

- explore, interpret, and make conjectures about everyday probability situations by estimating probabilities, conducting experiments, beginning to construct and conduct simulations, and analysing claims which they see and hear

G1 predict probabilities as either close to 0 , near 1 , or near $1 / 2$
G2 cite examples of everyday events with very high or very low probabilities
G3 predict whether one simple outcome is more or less likely than another
G4 use fractions to describe experimental probabilities

- determine theoretical probabilities using simple counting techniques
- demonstrate an understanding of the relationship between the numerical expression describing a probability and the events which give rise to the numbers


## Grade 5

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.
By the end of grade 6, students will be expected to Students will be expected to

- demonstrate an understanding of number A1 represent whole numbers to the millions meanings with respect to whole numbers, A2 interpret and model decimal tenths, hundredths, fractions, and decimals and thousandths
A3 interpret, model, and rename fractions
A4 demonstrate an understanding of the relationship between fractions and division
- explore integers, ratios, and percents in

A5 explore the concepts of ratio and rate informally common meaningful situations

- read and write whole numbers and decimals and demonstrate an understanding of place value (to millions and to thousandths)
- order whole numbers, fractions, and decimals and represent them in multiple ways

A6 read and represent numbers to millions
A7 read and represent decimals to thousandths

A8 compare and order large numbers
A9 compare and order decimals
A10 compare and order fractions using conceptual methods

- apply number theory concepts (e.g., prime numbers, factors) in relevant situations with respect to whole numbers, fractions, and decimals

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 6, students will be expected to Students will be expected to

- model problem situations involving whole numbers and decimals by selecting appropriate operations and procedures

B1 find sums and differences involving decimals to thousandths
B2 multiply 2-, 3-, and 4-digit numbers by 1-digit numbers
B3 find the product of two 2-digit numbers
B4 divide 2-, 3-, and 4 -digit numbers by single-digit divisors and investigate division by 2 -digit divisors
B5 find simple products of whole numbers and decimals
B6 divide decimal numbers by single-digit whole numbers

- model problem situations involving the addition and subtraction of simple fractions


## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- explore algebraic situations informally
- apply computational facts and procedures (algorithms) in a wide variety of problem situations involving whole numbers and decimals
- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers and decimals
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

B7 determine whether an open sentence is always, sometimes, or never true

B8 solve and create addition and subtraction problems involving whole number and/or decimals
B9 solve and create multiplication and division problems involving whole numbers and/or decimals

B10 estimate sums and differences involving decimals to thousandths
B11 estimate products and quotients of two whole numbers
B12 estimate products and quotients of decimals by single-digit whole numbers

B13 perform appropriate mental multiplications with facility
B14 divide numbers mentally when appropriate
B15 multiply whole numbers mentally by $0.1,0.01$, 0.001

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

By the end of grade 6 , students will be expected to

## Students will be expected to

- describe, extend, and create a wide variety of patterns and relationships to model and solve problems involving real-world situations and mathematical concepts
- explore how a change in one quality in a relationship affects another
- represent mathematical patterns and relationships in a variety of ways (including rules, tables, and one- and two-dimensional graphs)

C1 use place value patterns to extend understanding of the representation of numbers to millions
C2 recognize and explain the patterns in dividing by 10,100 , and 1000 and/or in multiplying by 0.1 , 0.01, 0.001

C3 solve problems using patterns
C4 rearrange factors to make multiplication simpler
C5 recognize how a change in one factor affects a product or quotient
C6 predict how a change in unit affects an SI measurement
C7 manipulate the dimensions of a rectangle so that the area remains the same

C8 demonstrate an understanding that the multiplicative relationship between numerators and denominators is constant for equivalent fractions
C9 represent measurement relationships using tables and two-dimensional graphs

- solve linear equations using informal, nonalgebraic methods


## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 6 , students will be expected to

- extend understanding of measurement concepts and attributes to include volume, temperature, perimeter, and angle
- communicate using standard units, understand the relationship among commonly used SI units (e.g., mm, cm, m, km ) and select appropriate units in given situations
- estimate and apply measurement concepts and skills in relevant problem situations and select and use appropriate tools and units
- develop and apply rules and procedures for determining measures (using concrete and graphing models)

Students will be expected to
D1 solve simple problems involving the perimeters of polygons
D2 calculate areas of irregular shapes
D3 determine the measures of right angles, acute angles and obtuse angles

D4 demonstrate an understanding of the relationships among particular SI units

D6 solve simple problems involving volume and capacity
D7 estimate angle size in degrees
D8 determine which unit is appropriate in a given situation and solve problems involving length and area

D5 develop formulas for areas and perimeters of squares and other rectangles

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 6, students will be expected to

- identify, draw, and build physical models of geometric figures
- solve problems using geometric relationships and spatial reasoning


## Students will be expected to

E1 draw a variety of nets for different prisms and pyramids
E2 identify, describe, and represent the various crosssections of cubes and rectangular prisms
E3 make and interpret isometric drawings of shapes made from cubes
E4 explore relationships between area and perimeter of squares and rectangles
E5 predict and construct figures made by combining two triangles

- describe, model, and compare 2- and 3-D figures and shapes, explore their properties, and classify them in alternate ways

E6 recognize, name, describe, and represent
perpendicular lines/segments, bisectors of angles and segments, and perpendicular-bisectors of segments
E7 recognize, name, describe, and construct right, obtuse, and acute triangles
E8 make generalizations about the diagonal properties of squares and rectangles and apply these properties

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships. (continued)

- investigate and predict the results of transformations and begin to use them to compare shapes and explain geometric concepts (e.g., symmetry and similarity)

E9 make generalizations about the properties of translations and reflections and apply these properties
E10 explore rotations of one-quarter, one-half, and three-quarter turns using a variety of centres
E11 make generalizations about the rotational symmetry property of squares and rectangles and apply them
E12 recognize, name, and represent figures that tessellate
E13 explore how figures can be dissected and transformed into other figures

GCO F: Students will solve problems involving the collection, display, and analysis of data.
By the end of grade 6, students will be expected to Students will be expected to

- collect, organize, describe relevant data in multiple ways construct a variety of data displays (including tables, charts, and graphs) and consider their relative appropriateness
- read, interpret, and make and modify predictions from displays of relevant data
- develop and apply measures of central tendency (mean, median, and mode)
- formulate and solve simple problems (both real-world and from other academic disciplines) that involve the collection, display, and analysis of data and explain conclusions which may be drawn

F1 use double bar graphs to display data
F2 use pictographs and bar graphs to display and interpret data
F3 use coordinate graphs to display data
F4 create and interpret line graphs
F5 group data appropriately and use stem-and-leaf plots to describe the data

F6 recognize and explain the effect of certain changes in data on the mean of that data

F7 explore relevant issues for which data collection assists in reaching conclusions

## GCO G: Students will represent and solve problems involving uncertainty.

By the end of grade 6, students will be expected to

- explore, interpret, and make conjectures about everyday probability situations by estimating probabilities, conducting experiments, beginning to construct and conduct simulations, and analysing claims which they see and hear
- determine theoretical probabilities using simple counting techniques
- demonstrate an understanding of the relationship between the numerical expression describing a probability and the events which give rise to the numbers


## Students will be expected to

G1 conduct simple experiments to determine experimental probabilities

G2 determine simple theoretical probabilities, and use fractions to describe them

## Grade 6

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO A: Students will demonstrate number sense and apply number theory concepts.

## By the end of grade 6, students will be expected to

- demonstrate an understanding of number meanings with respect to whole numbers, fractions, and decimals
- explore integers, ratios, and percents in common meaningful situations
- read and write whole numbers and decimals and demonstrate an understanding of place value (to millions and to thousandths)
- order whole numbers, fractions, and decimals and represent them in multiple ways
- apply number theory concepts (e.g., prime numbers, factors) in relevant situations with respect to whole numbers, fractions, and decimals


## Students will be expected to

A1 represent large numbers in a variety of forms
A2 represent fractions and decimals

A3 write and interpret ratios, comparing part-to-part and part-to-whole
A4 demonstrate an understanding of equivalent ratios
A5 demonstrate an understanding of the concept of percent as a ratio
A6 demonstrate an understanding of the meaning of a negative integer

A7 read and write whole numbers in a variety of forms A8 demonstrate an understanding of the place-value system

A9 relate fractional and decimal forms of numbers

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations.

By the end of grade 6, students will be expected to

- model problem situations involving whole numbers and decimals by selecting appropriate operations and procedures
- model problem situations involving the addition and subtraction of simple fractions
- explore algebraic situations informally


## Students will be expected to

B1 compute products of whole numbers and decimals B2 model and calculate the products of two decimals B3 compute quotients of whole numbers and decimals
B4 model and calculate the quotients of two decimals
B5 add and subtract simple fractions using models

B6 demonstrate an understanding of the function nature of input-output situations

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO B: Students will demonstrate operation sense and apply operation principles and procedures in both numeric and algebraic situations. (continued)

- apply computational facts and procedures (algorithms) in a wide variety of problem situations involving whole numbers and decimals
- apply estimation techniques to predict, and justify the reasonableness of, results in relevant problem situations involving whole numbers and decimals
- select and use appropriate computational techniques (including mental, paper-andpencil, and technological) in given situations

B7 solve and create relevant addition, subtraction, multiplication, and division problems involving whole numbers
B8 solve and create relevant addition, subtraction, multiplication and division problems involving decimals

B9 estimate products and quotients involving whole numbers only, whole numbers and decimals, and decimals only
B11 calculate sums and differences in relevant contexts by using the most appropriate method

B10 divide numbers by $0.1,0.01$, and 0.001 mentally
B12 calculate products and quotients in relevant contexts by using the most appropriate method

GCO C: Students will explore, recognize, represent, and apply patterns and relationships, both informally and formally.

By the end of grade 6 , students will be expected to

- describe, extend, and create a wide variety of patterns and relationships to model and solve problems involving real-world situations and mathematical concepts
- explore how a change in one quality in a relationship affects another
- represent mathematical patterns and relationships in a variety of ways (including rules, tables, and one- and two-dimensional graphs)


## Students will be expected to

C1 solve problems involving patterns
C2 use patterns to explore division by $0.1,0.01$, and 0.001

C3 recognize and explain how changes in base or height will affect areas of rectangles, parallelograms, or triangles
C4 recognize and explain how an increase in height, width, or length of a rectangular prism changes its volume
C5 recognize and explain how the change in one term of a ratio affects the other term

C6 represent equivalent ratios using tables and graphs
C7 represent square and triangular numbers concretely, pictorially, and symbolically
C8 solve simple linear equations using open frames
C9 demonstrate understanding of the use of letters to replace open frames

- solve linear equations using informal, nonalgebraic methods


## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO D: Students will demonstrate an understanding of and apply concepts and skills associated with measurement.

By the end of grade 6, students will be expected to Students will be expected to

- extend understanding of measurement concepts and attributes to include volume, temperature, perimeter, and angle
- communicate using standard units, understand the relationship among commonly used SI units (e.g., mm, cm, m, km ) and select appropriate units in given situations

D1 use the relationship among particular SI units to compare objects
D2 describe mass measurements in tonnes
D3 demonstrate an understanding of the relationship between capacity and volume

- estimate and apply measurement concepts and skills in relevant problem situations and select and use appropriate tools and units

D4 estimate and measure angles using a protractor
D5 draw angles of a given size
D6 continue to solve measurement problems involving length, capacity, area, volume, mass, and time

- develop and apply rules and procedures for determining measures (using concrete and graphing models)

D7 demonstrate an understanding of the relationships among the base, height, and area of a parallelogram
D8 demonstrate an understanding of the relationship between the area of a triangle and the area of a related parallelogram
D9 demonstrate an understanding of the relationship among the three dimensions of a rectangular prism and its volume and its surface area

## GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships.

By the end of grade 6 , students will be expected to

- identify, draw, and build physical models of geometric figures
- solve problems using geometric relationships and spatial reasoning
- describe, model, and compare 2- and 3-D figures and shapes, explore their properties, and classify them in alternate ways


## Students will be expected to

E1 describe and represent the various cross-sections of cones, cylinders, pyramids, and prisms
E2 make and interpret orthographic drawings of 3-D shapes made with cubes

E3 make and apply generalizations about the sum of the angles in triangles and quadrilaterals
E4 make and apply generalizations about the diagonal properties of trapezoids, kites, parallelograms, and rhombi
E5 sort the members of the quadrilateral "family" under property headings
E6 recognize, name, describe, and represent similar figures

## Key-Stage Curriculum Outcomes Specific Curriculum Outcomes

GCO E: Students will demonstrate spatial sense and apply geometric concepts, properties, and relationships. (continued)

- investigate and predict the results of transformations and begin to use them to compare shapes and explain geometric concepts (e.g., symmetry and similarity)

E7 make generalizations about the planes of symmetry of 3-D shapes
E8 make generalizations about the rotational symmetry property of all members of the quadrilateral "family" and of regular polygons
E9 recognize and represent dilatation images of 2-D figures and make connections to similar figures
E10 predict and represent the result of combining transformations

GCO F: Students will solve problems involving the collection, display, and analysis of data.

By the end of grade 6, students will be expected to

- collect, organize, and describe relevant data in multiple ways
- construct a variety of data displays (including tables, charts, and graphs) and consider their relative appropriateness
- read, interpret, and make and modify predictions from displays of relevant data
- develop and apply measures of central tendency (mean, median, and mode)
- formulate and solve simple problems (both real-world and from other academic disciplines) that involve the collection, display, and analysis of data and explain conclusions which may be drawn

Students will be expected to
F1 choose and evaluate approp riate samples for data collection
F2 identify various types of data sources
F3 plot coordinates in four quadrants
F4 use bar graphs, double bar graphs, and stem-andleaf plots to display data
F5 use circle graphs to represent data proportionally
F6 interpret data represented in scatterplots
F7 make inferences from data displays
F8 demonstrate an understanding of the differences among mean, median, and mode

F9 explore relevant issues for which data collection assists in reaching conclusions

GCO G: Students will represent and solve problems involving uncertainty.

## By the end of grade 6, students will be expected to

- explore, interpret, and make conjectures about everyday probability situations by estimating probabilities, conducting experiments, beginning to construct and conduct simulations, and analysing claims which they see and hear
- determine theoretical probabilities using simple counting techniques
- demonstrate an understanding of the relationship between the numerical expression describing a probability and the events which give rise to the numbers


## Students will be expected to

G1 conduct simple simulations to determine probabilities
G2 evaluate the reliability of sampling results
G3 analyse simple probabilistic claims

G4 determine theoretical probabilities
G5 identify events that could be associated with a particular theoretical probability

