

$$e = \frac{\text{what you get out}}{\text{what you pay for}} = \frac{W_{\text{out}}}{Q_H} = 1 - \frac{Q_C}{Q_H}$$

definition of efficiency and formula for a heat engine

$$e_{\text{max}} = 1 - \frac{T_C}{T_H}$$

the maximum or Carnot efficiency of a heat engine

$$\Delta S_{\text{system}} = 0$$

$$\Delta S = \pm \frac{Q}{T}$$

entropy change associated with heat

$$k_B = 1.38 \times 10^{-23} \text{ J/K} = \frac{R}{N_A}$$

Boltzmann's constant and its relationship to the gas constant $R = 8.31 \text{ J/K}$ and Avogadro's Number $N_A = 6.02 \times 10^{23}$

$$pV = Nk_B T = nRT$$

ideal gas law, N is the number of molecules, n is the number of moles, T is in Kelvin

$$E_{th} = \frac{3}{2} Nk_B T$$

for a monatomic gas, also works with ΔE_{th} and ΔT

$$\Delta E_{th} = W_{in} + Q_{in}$$

1st Law of Thermodynamics, you need to modify the signs if you are talking about W_{out} or Q that is "leaving" the system

$$\Delta S_{\text{system}} \geq 0$$

2nd Law of Thermodynamics for an isolated system, could also say state of disorder increases with time

$$v_{rms} = \sqrt{\frac{3k_B T}{m}}$$

the average velocity of an atom in a gas at temperature T . Can find m from molecular weight (in kg) divided by $N_A = 6.02 \times 10^{23}$.

$$E_{th} = NK_{avg} = N\left(\frac{1}{2}mv_{rms}^2\right) = \frac{3}{2}Nk_B T$$

for a monatomic gas the thermal energy represents that the total kinetic energy of the molecules which is proportional to v_{rms}^2 and T

$$p = \frac{F}{A}$$

definition of pressure, units are Pascals (Pa) when F is in Newtons and A is in m^2

$$W_{\text{gas, out}} = p\Delta V = \text{"area under } pV \text{ curve"}$$

an *expanding* gas does work on its environment. If the pressure is constant then you may use the simple ΔV expression, otherwise it is the area

$$p_i = p_f$$

an isobaric or constant pressure process

$$V_i = V_f$$

a constant volume process $W_{\text{out}} = 0$

$$T_i = T_f$$

an isothermal process $\Delta E_{th} = 0$

$$p_i V_i^{\frac{5}{3}} = p_f V_f^{\frac{5}{3}}$$

an adiabatic process $Q = 0$ and $\Delta S = 0$

$$\frac{p_i V_i}{T_i} = \frac{p_f V_f}{T_f}$$

once you have identified the process you can use this formula, a form of the ideal gas law if N is constant

$$\rho = \frac{m}{V}$$

definition of density, use m in kg and V in m^3 . $1 \text{ m}^3 = 1000 \text{ L} = 10^6 \text{ cm}^3 = 10^6 \text{ mL}$

$$p = p_0 + \rho_f g d$$

pressure in a fluid of density ρ_f as a function of depth. p_0 is a "reference pressure" where $d = 0$. This equation also supports *Pascal's principle*: if the pressure changes at one point in the fluid it changes by the same amount at every other point.

$$p_{\text{atmos}} = 101.3 \text{ kPa} = 1 \text{ atm}$$

atmospheric pressure

$$F_B = \rho_f V_f g$$

buoyant force directed upward. V_f is the volume of fluid displaced and it equal to the volume of the object *if* the object is submerged. Object will also experience the force of gravity *weight* $w = mg$ directed downward.

$$\rho_{\text{avg}} = \rho_f$$

neutral buoyancy $F_B = w$

$$v_1 A_1 = v_2 A_2$$

equation of continuity for an incompressible fluid

$$Q = vA = \frac{\Delta V}{\Delta t}$$

volume flow rate in m^3/s

$$p_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2 = p_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1$$

Bernoulli's equation. Often used to find a pressure difference $p_2 - p_1$. If the fluid is low density (like air) and the change in y is small you can drop the $\rho g y$ terms.

$$\omega = 2\pi f = \frac{2\pi}{T}$$

relationship between radial frequency ω , frequency f and period T

$$x(t) = A \cos(\omega t) = A \cos(2\pi t) = A \cos(2\pi \frac{t}{T})$$

the motion of an object in simple harmonic motion. For vertical mass spring system substitute $y(t)$ for a pendulum either $\theta(t)$ or $s(t)$ (the arc length). $x_{\text{max}} = A$. If you need to calculate an actual x at some time make sure you take the cosine in radians.

$$v_x(t) = -A\omega \sin(\omega t)$$

velocity as a function of time. $v_{\text{max}} = A\omega$. Substitute in frequency f and period T as necessary.

$$a_x(t) = -A\omega^2 \cos(\omega t) = -\omega^2 x(t)$$

acceleration as a function of time. Substitute in frequency f and period T as necessary.

$$\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{g}{L}}$$

radial frequency for mass-spring and pendulum systems

$$T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{L}{g}}$$

period for mass-spring and pendulum systems

$$E = K + U = \frac{1}{2}mv(t)^2 + \frac{1}{2}kx(t)^2$$

energy relationships in a simple harmonic oscillator

$$K_{\text{max}} = U_{\text{max}} = \frac{1}{2}m(v_{\text{max}})^2 = \frac{1}{2}kA^2$$

max energies

$$x_{\text{max}}(\text{at } t = \tau) = Ae^{-1} \approx 0.37A$$

how to find the time constant τ that describes the decay of oscillations in a damped system

$$y(x, t) = A \cos\left(2\pi\left(\frac{x}{\lambda} - \frac{t}{T}\right)\right)$$

sinusoidal wave moving to the right (change to positive sign for wave to the left)

$$v = f\lambda = \frac{\lambda}{T} = \frac{\Delta x}{\Delta t}$$

basic relationship between speed, frequency, period, and wavelength. Use the "quotes" form to relate history and snapshot graphs.

$$v_{\text{sound}} = \sqrt{\frac{\gamma k_B T}{m}} = \sqrt{\frac{\gamma RT}{M}}$$

speed of sound $\gamma = 3/2$ for monatomic gases, $5/2$ for diatomic

$$v_{\text{string}} = \sqrt{\frac{T_s}{\mu}}$$

waves on a string, T_s is tension, μ is *linear* density

$$v_{\text{light}} = c = 3.00 \times 10^8 \text{ m/s}$$

speed of electromagnetic waves in vacuum (including light, radio waves)