

$\Delta x = x_f - x_i$	for any scalar/vector in place of $x$		$\vec{C} = \vec{A} + \vec{B}$
$\vec{d}_{\text{net}} = \vec{d}_1 + \vec{d}_2$	Knight's version for vector displacement		
$\Delta \vec{x} = \vec{x}_f - \vec{x}_i$	Carl's version for vector displacement		$\vec{C} = \vec{A} - \vec{B}$
$v_x = \frac{\Delta x}{\Delta t}$	definition of 1-D (instantaneous) velocity, take a slope of $x(t)$	$\vec{A} = \vec{A}_x + \vec{A}_y$	decomposing a vector into components
$a_x = \frac{\Delta v_x}{\Delta t}$	definition of acceleration, take a slope of $v_x(t)$	$ \vec{A}  \equiv \text{mag. or length of } \vec{A}$	quantity is always positive, sometimes just called $A$
$\Delta x = v_x \Delta t \leftrightarrow A = hw$	displacement as area under $v_x(t)$ curve	$\vec{A} = \vec{A}_{xR} + \vec{A}_{yR}$	decomposing a vector into ramp components
$\Delta v = a_x \Delta t \leftrightarrow A = hw$	change in $v_x$ as area under $a_x(t)$ curve	$a_{xR} = \pm g \sin \theta$	acceleration of free object on a ramp
$\Delta x = (v_x)_i \Delta t + \frac{1}{2} \Delta v_x \Delta t$	displacement as area under a linear $v_x(t)$ curve	$\Delta y_R = v_{yR} = a_{yR} = 0$	no motion in $y_R$ direction
$x_f = x_i + v_x \Delta t$	kin. formula for constant velocity	$\vec{v}_{AC} = \vec{v}_{AB} + \vec{v}_{BC}$	subscript rule for relative velocities (Galilean transformation)
$y = mx + b$	high school formula for a straight line	$(v_x)_i =  \vec{v}_i  \cos \theta$ $(v_y)_i =  \vec{v}_i  \sin \theta$	initial velocity components for a launched projectile
$x_f = x_i + (v_x)_i \Delta t + \frac{1}{2} a_x (\Delta t)^2$	kin. formula for displacement with constant accel. aka formula 2.12	$x_f = x_i + (v_x)_i \Delta t$	projectile, uniform $x$ -motion
$(v_x)_f = (v_x)_i + a_x \Delta t$	kin. formula for velocity with constant accel. aka 2.11	$(v_x)_f = (v_x)_i$	projectile, constant $v_x$ , $a_x = 0$
$(v_x)_f^2 = (v_x)_i^2 + 2a_x \Delta x$	the "no-time" formula for constant accel. aka 2.13	$y_f = y_i + (v_y)_i \Delta t - \frac{1}{2} g (\Delta t)^2$	projectile, $y$ -displacement, $a_y = -g$
$a_y = -g = -9.80 \text{ m/s}^2$	free-fall acceleration due to gravity	$(v_y)_f = (v_y)_i - g \Delta t$	projectile, decreasing $v_y$
$\sin \theta = \frac{\text{opps}}{\text{hyp}}, \cos \theta = \frac{\text{adj}}{\text{hyp}}$ $\tan \theta = \frac{\text{opps}}{\text{adj}}$	high school trig formulas	$f = \frac{1}{T}$	relationship between frequency and period
$(\text{hyp})^2 = (\text{adj})^2 + (\text{opps})^2$	Pythagoras' theorem (right angle triangles)	$v = \frac{2\pi r}{T} = 2\pi r f$	orbital speed (velocity changes)
$c^2 = a^2 + b^2 - 2ab \cos(\angle C)$	law of cosines for side $c$ opposite $\angle C$	$\vec{a} = \left( \frac{v^2}{r}, \text{toward centre} \right)$	centripetal acceleration
$\vec{v} = \frac{\vec{d}}{\Delta t} = \frac{\Delta \vec{x}}{\Delta t}$	definition of velocity in 2 or more dimensions in terms of displacement vector $\vec{d}$ or $\Delta \vec{x}$	$\vec{F}_{\text{net}} = \vec{0} \Rightarrow \vec{v}$ is constant	Newton's 1 <sup>st</sup> law, constant may or may not be 0
$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$	definition of acceleration in 2 or more dimensions	$\vec{v}$ is constant $\Rightarrow \vec{F}_{\text{net}} = \vec{0}$	Newton's 1 <sup>st</sup> law stated in converse form
		$\vec{a} = \frac{\vec{F}_{\text{net}}}{m}$ or $\vec{F}_{\text{net}} = m\vec{a}$	Newton's 2 <sup>nd</sup> law, definition of mass
		$\vec{F}(\text{B on A}) = -\vec{F}(\text{A on B})$	Newton's 3 <sup>rd</sup> law
		$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 + \dots = \Sigma \vec{F}_i$	forces sum to produce net force

$w_{\text{apparent}} = m(g + a_y)$	apparent weight <i>if you are</i> upside up	$T^2 = \left(\frac{4\pi^2}{GM}\right) r^3 = kr^3$	Kepler's 3rd law. Use $k$ form when comparing orbiting objects.
$w_{\text{apparent}} = -m(g + a_y)$	apparent weight <i>if you are</i> upside down	$\theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2$	an example of an "angular" kinematic equation
$n = w_{yR} = mg \cos \theta$	magnitude of normal force for a ramp	$a_{\text{tan}} = \alpha r$	tangential component of acceleration
$f_{s,\text{max}} = \mu_s n$	magnitude of maximum static friction	$\tau = \pm r F_{\perp} = \pm r_{\perp} F = \pm r F \sin \phi$	torque about a pivot, choose pos. sign for CCW
$f_k = \mu_k n$	magnitude of kinetic friction $\vec{f}_k$ is opposite to direction of $\vec{v}$	$\tau_{\text{net}} = \tau_1 + \tau_2 + \dots = \Sigma \tau_i$	summing torques
$f_r = \mu_r n$	rolling friction	$x_{cg} = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3 + \dots}{m_1 + m_2 + m_3 + \dots}$	centre of gravity in $x$ , similar expression for $y_{cg}$
$D = \frac{1}{2} C_D \rho A v^2$	empirical law for drag force in air	$I = \Sigma m_i r_i^2$	moment of inertia, depends on choice of centre
$F = T$	tension in a massless string or rope provides a force	$\alpha = \frac{\tau_{\text{net}}}{I}$	Newton's 2nd law for rotation
$ \vec{T}_1  =  \vec{T}_2 $	magnitude of tension constant for massless pulley	$I = MR^2$	moment of inertia for a hoop
$F_{\text{centripetal}} = \frac{mv^2}{r}$	a net force directed toward the centre	$I = \frac{1}{2} MR^2$	moment of inertia for a disc or cylinder
$F_{\text{grav}} = \frac{Gm_1 m_2}{r^2}$	Newton's inverse square law for gravitation; $G = 6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$	$I = \frac{2}{5} MR^2$	moment of inertia for a solid sphere
$(F_{\text{sp}})_x = -k \Delta x$	Hooke's Law for a spring	$a_{\text{obj}} = \alpha R$	example of a constraint equation for a pulley of radius $R$
$s = r \theta$	arc length $s$ , only true if $\theta$ is in radians	$v = \omega R$	rolling constraint, rolling object as a whole moves at $v$
$2\pi \text{ radians} = 360^\circ = 1 \text{ rev}$	relations between angular units	$v_{\text{top}} = 2v, v_{\text{bottom}} = 0$	speeds at top and bottom of a rolling object
$\omega = \frac{\Delta \theta}{\Delta t} = \frac{2\pi}{T} = \frac{\pi}{30} \text{ (rpm)}$	positive if motion is CCW	$F_{x,\text{net}} = F_{y,\text{net}} = \tau_{\text{net}} = 0$	conditions for static equilibrium of extended object, choose any pivot point
$v = \omega r$	this is tangential or orbital motion, $\vec{v}$ changes	$\theta_c = \tan^{-1} \left( \frac{t}{2h} \right)$	critical tipping angle if c.o.g. is height $h$ above and centred over a base of width $t$
$a_{\text{centri}} = \frac{v^2}{r} = \omega^2 r$	$\vec{a}_{\text{centri}}$ is always directed towards the centre of the circle	$\vec{P}_i = \vec{P}_f$	conservation of momentum for no external forces
$v_{\text{orbit}} = \sqrt{gr}$	a freefalling object in circular orbit; $g$ is not 9.80 if not at earth's surface	$L = I\omega$	angular momentum
$g = \frac{GM}{r^2}$	a generalized gravitational acceleration near a "planet" with mass $M$	$\vec{J} = (\vec{F}_{\text{net}})_{\text{avg}} \Delta t = \vec{p}_f - \vec{p}_i$	impulse defined and impulse-momentum theorem
$\alpha = \frac{\Delta \omega}{\Delta t}$	angular acceleration	$\vec{p} = m\vec{v}$	momentum defined

$\vec{P} = \sum_i m_i \vec{v}_i$	system momentum
$L_{\text{system}} = \sum I_i \omega_i$	system angular momentum
$(L_{\text{system}})_i = (L_{\text{system}})_f$	conservation of angular momentum for no external torques
$\Delta L = (\tau_{\text{net}})_{\text{avg}} \Delta t$	angular impulse-momentum theorem
$E = K + U_g + U_s + E_{\text{th}} + E_{\text{chem}} + \dots$	total energy of a system
$\Delta E = \Delta K + \Delta U_g + \Delta U_s + \Delta E_{\text{th}} + \Delta E_{\text{chem}} + \dots$	total energy <i>change</i> of a system
$W = \Delta E$	work-energy theorem; work done “on” the system represents only energy input
$W = F_{\text{ext}} d \cos \theta = F_{\text{ext}} \Delta x \cos \theta$	work done on the system by a force external to the system, not $F_{\text{net}}$
$K = \frac{1}{2} m v^2$	kinetic energy from translation, will also work for a point object moving in a circle
$K = \frac{1}{2} I \omega^2$	kinetic energy for a rotating rigid body
$U_g = mgy$	gravitational potential energy for constant $g$ , you have chosen a potential=0 point at $y = 0$
$U_s = \frac{1}{2} k x^2$	$x$ is the extension of the spring
$\Delta E_{\text{th}} = f_k  \Delta x $	thermal energy for a dragged object
$(v_{1x})_f = \frac{m_1 - m_2}{m_1 + m_2} (v_{1x})_i$	final velocity for the colliding particle in a 1-D elastic collision
$(v_{2x})_f = \frac{2m_1}{m_1 + m_2} (v_{1x})_i$	final velocity for the target particle in a 1-D elastic collision
$P = \frac{W}{\Delta t} = F_{\text{ext}} v \cos \theta$	power
efficiency, $e = \frac{\text{what you get}}{\text{what you had to pay}}$	efficiency in energy transfer
$E_{\text{th}} = \frac{3}{2} N k_B T = \frac{3}{2} N_{\text{mole}} R T$	$k_B = 1.38 \times 10^{-23}$ J/K, for a monatomic gas, $T$ in Kelvin

