

$$\left. \begin{aligned} x'(x, y, z, t) &= x - vt \\ y'(x, y, z, t) &= y \\ z'(x, y, z, t) &= z \\ t'(x, y, z, t) &= t \end{aligned} \right\} \text{Galilean transforms} \quad (1)$$

$$\left. \begin{aligned} x'(x, y, z, t) &= \gamma(x - vt) \\ y'(x, y, z, t) &= y \\ z'(x, y, z, t) &= z \\ t'(x, y, z, t) &= \gamma\left(t - \frac{vx}{c^2}\right) \end{aligned} \right\} \text{Lorentz transforms} \quad (2)$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{1}{\sqrt{1 - \beta^2}} \quad (3)$$

$$\begin{pmatrix} ct' \\ x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} \gamma & -\beta\gamma & 0 & 0 \\ -\beta\gamma & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} ct \\ x \\ y \\ z \end{pmatrix} \quad (4)$$

The Lorentz transform also works with the energy-momentum 4-vector: $(p_0, p_1, p_2, p_3) = (E/c, p_x, p_y, p_z)$.

$$u'_x = \frac{dx'}{dt'} = \frac{u_x - v}{1 - \frac{u_x v}{c^2}} \quad (5)$$

$$u'_y = \frac{dy'}{dt'} = \frac{u_y}{\gamma(1 - \frac{u_x v}{c^2})} \quad (6)$$

To obtain the inverse transformations simply switch primed and unprimed and replace v with $-v$ in the formulas above.

$$\Delta t = \gamma\tau \quad (7)$$

$$L = \frac{L_0}{\gamma} \quad (8)$$

$$(\Delta s)^2 = (c\Delta t)^2 - (\Delta x)^2 - (\Delta y)^2 - (\Delta z)^2 \quad (9)$$

$$(\Delta s')^2 = (\Delta s)^2 \quad (10)$$

$$(\text{slope of } x'\text{-axis}) = \beta \quad (11)$$

$$(\text{slope of } ct'\text{-axis}) = \frac{1}{\beta} \quad (12)$$

$$E = mc^2 + E_K = p_0 c = \frac{mc^2}{\sqrt{1 - \frac{u^2}{c^2}}} \text{ if } m \neq 0 \quad (13)$$

$$\vec{p} = (p_1, p_2, p_3) = \frac{m\vec{u}}{\sqrt{1 - \frac{u^2}{c^2}}} \text{ if } m \neq 0 \quad (14)$$

$$E^2 = p^2 c^2 + m^2 c^4 \text{ for both } m = 0 \text{ and } m \neq 0 \quad (15)$$

$$c = 3.00 \times 10^8 \text{ m/s} \quad m(\text{electron}) = 9.11 \times 10^{-31} \text{ kg} = 5.11 \times 10^5 \text{ eV}/c^2$$

$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4} \quad k_B = 1.38 \times 10^{-23} \text{ J/K} = 8.63 \times 10^{-5} \text{ eV/K}$$

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J} \quad e = 1.60 \times 10^{-19} \text{ C}$$

$$hc = 1240 \text{ eV}\cdot\text{nm}$$