

Physical Constants and Conversion Factors

$$R = 8.3145 \text{ J K}^{-1} \text{ mol}^{-1} = 0.083145 \text{ L bar K}^{-1} \text{ mol}^{-1} = 0.082058 \text{ L atm K}^{-1} \text{ mol}^{-1}$$

$$N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$$

$$k_B = R/N_A$$

$$T/K = t/^\circ\text{C} + 273.15$$

$$1 \text{ bar} = 10^5 \text{ Pa}$$

$$1 \text{ atm} = 1.01325 \text{ bar}$$

$$1 \text{ mm Hg} = 133.32 \text{ Pa}$$

$$1 \text{ L bar} = 100 \text{ J}$$

$$1 \text{ m}^3 = 1000 \text{ L}$$

$$1 \text{ L} = 1000 \text{ cm}^3$$

First Law

$$dU = dq + dw$$

$$\Delta U = q + w$$

$$\Delta U = U_f - U_i$$

$$\Delta U = w_{\text{adiabatic}}$$

$$(\Delta U = 0)_{\text{isolated system}}$$

$$0 = \oint dU \quad (\text{cyclic process})$$

$$dw = -p_{\text{external}} dV \quad (\text{expansion/compression work})$$

$$w = - \int_{V_i}^{V_f} p_{\text{external}} dV$$

$$p = p_{\text{external}} \quad (\text{reversible})$$

$$p < p_{\text{external}} \quad (\text{irrev. compression})$$

$$p > p_{\text{external}} \quad (\text{irrev. expansion})$$

$$w_{\text{rev}} = - \int_{V_i}^{V_f} p dV$$

$$w_{\text{rev(const., } p)} = -p(V_f - V_i)$$

$$w_{\text{irrev(const., external } p)} = -p_{\text{external}}(V_f - V_i)$$

$$H = U + PV$$

$$\Delta H = H_f - H_i$$

$$\Delta H = \Delta U + \Delta(pV) = U_f - U_i + p_f V_f - p_i V_i$$

$$C_V = \frac{dq_V}{dT} = \left(\frac{\partial U}{\partial T} \right)_V$$

$$C_p = \frac{dq_p}{dT} = \left(\frac{\partial H}{\partial T} \right)_p$$

$$C_p - C_V = T \left(\frac{\partial p}{\partial T} \right)_V \left(\frac{\partial V}{\partial T} \right)_p = \frac{\beta^2 VT}{\kappa}$$

$$q_V = \Delta U_V = \int_{T_i}^{T_f} C_V dT$$

$$q_p = \Delta H_p = \int_{T_i}^{T_f} C_p dT \quad (\text{only } p-V \text{ work})$$

$$\beta = V^{-1}(\partial V/\partial T)_p = -\rho^{-1}(\partial \rho/\partial T)_p$$

$$\kappa = \kappa_T = -V^{-1}(\partial V/\partial p)_T = \rho^{-1}(\partial \rho/\partial p)_T$$

$$\beta_{\text{linear}} = \beta/3 = \ell^{-1}(\partial \ell/\partial T)_p$$

$$(\partial p/\partial T)_V = \beta/\kappa$$

$$\mu_{\text{JT}} = (\partial T/\partial p)_H = -V_m(1 - \beta T)/C_{pm}$$

$$dU = \left(\frac{\partial U}{\partial T} \right)_V dT + \left(\frac{\partial U}{\partial V} \right)_T dV = C_V dT + \left(\frac{\beta T}{\kappa} - p \right) dV \quad \left(\frac{\partial U}{\partial V} \right)_T = T \left(\frac{\partial p}{\partial T} \right)_V - p = \frac{\beta T}{\kappa} - p$$

$$dH = \left(\frac{\partial H}{\partial T} \right)_p dT + \left(\frac{\partial H}{\partial p} \right)_T dp = C_p dT + V(1 - \beta T) dp$$

$$\left(\frac{\partial H}{\partial p} \right)_T = V(1 - \beta T)$$

$$\left[\frac{\partial}{\partial x} \left(\frac{\partial f}{\partial y} \right)_x \right]_y = \left[\frac{\partial}{\partial y} \left(\frac{\partial f}{\partial x} \right)_y \right]_x$$

$$\left(\frac{\partial f}{\partial y} \right)_x = \frac{1}{\left(\frac{\partial y}{\partial f} \right)_x}$$

$$\left(\frac{\partial f}{\partial x} \right)_y = - \left(\frac{\partial f}{\partial x} \right)_y \left(\frac{\partial x}{\partial y} \right)_f$$

$$du = g(x, y)dx + h(x, y)dy$$

du is exact and the function $u(x, y)$ exists if

$$\left(\frac{\partial g}{\partial y} \right)_x = \left(\frac{\partial h}{\partial x} \right)_y$$

Ideal Gases

$$p = nRT/V$$

$$p_i = n_i RT/V$$

$$p_i/p = n_i/(n_1 + n_2 + n_3 + \dots) = x_i$$

$$p = Nk_B T/V$$

$$C_p - C_V = nR$$

$$C_{pm} - C_{Vm} = R$$

$$\beta = 1/T$$

$$\kappa = 1/p$$

$$(\partial U/\partial V)_T = 0$$

$$(\partial H/\partial p)_T = 0$$

$$(\partial C_V/\partial V)_T = 0$$

$$(\partial C_p/\partial p)_T = 0$$

$$\mu_{JT} = 0$$

$$dU = C_V dT$$

$$\Delta U = \int_{T_i}^{T_f} C_V dT$$

$$\Delta U (\text{const. } C_V) = C_V (T_f - T_i)$$

$$dH = C_p dT$$

$$\Delta H = \int_{T_i}^{T_f} C_p dT$$

$$\Delta H (\text{const. } C_p) = C_p (T_f - T_i)$$

$w = -nRT \ln(V_f/V_i)$ (reversible isothermal expansion/compression, variable pressure)

$w = -p(V_f - V_i) = -nR(T_f - T_i)$ (isothermal expansion/compression at constant pressure)

isothermal: $p_i V_i = p_f V_f$ and $(\partial p/\partial V)_T = -p/V$

adiabatic: $dU = C_V dT = dw$ and $\Delta U = w$ and $\int_{T_i}^{T_f} C_V dT = - \int_{V_i}^{V_f} p_{\text{external}} dV$

rev. adiabatic ($p = p_{\text{external}}$): $\int_{T_i}^{T_f} \frac{C_{Vm}}{T} dT = -R \int_{V_i}^{V_f} \frac{1}{V} dV$ and $C_{Vm} \ln(T_f/T_i) = -R \ln(V_f/V_i)$ (const. C_{Vm})

rev. adiabatic ($p = p_{\text{external}}$), $\gamma = C_{pm}/C_{Vm}$ constant: $p_i V_i^\gamma = p_f V_f^\gamma$ and $(\partial p/\partial V)_{\text{ad.}} = -\gamma p/V$

Real Gases

$$p = \frac{nRT}{V-nb} - \frac{n^2a}{V^2} = \frac{RT}{V_m-b} - \frac{a}{V_m^2}$$

$$\left(\frac{\partial U}{\partial V} \right)_T = \frac{a}{V_m^2}$$

$$Z = pV/nRT = pV_m/RT = p/p_{\text{ideal}}$$

$$Z = 1 + \frac{B(T)}{V_m} + \frac{C(T)}{V_m^2} + \frac{D(T)}{V_m^3} + \dots$$

$$B(T) = b - \frac{a}{RT}$$

$$T_{\text{Boyle}} = a/Rb$$

$$\mu_{JT} = \left(\frac{\partial T}{\partial p} \right)_H = \frac{1}{C_{pm}} \left(\frac{2a}{RT} - b \right)$$

Thermochemistry

$$q_p = \Delta H^\circ = \Delta H_f^\circ(\text{products}) - \Delta H_f^\circ(\text{reactants}) \quad w_p = -RT\Delta n_{\text{gas}} \quad \Delta U^\circ = \Delta H^\circ - RT\Delta n_{\text{gas}}$$

$$\Delta H = \sum_i v_i H_m(i) \quad \Delta C_p = \sum_i v_i C_{pm}(i) \quad \Delta U = \sum_i v_i U_m(i) \quad \Delta V = \sum_i v_i V_m(i)$$

$$\Delta H^\circ(T_2) = \Delta H^\circ(T_1) + \int_{T_1}^{T_2} \Delta C_p dT \quad \Delta H(p) = \Delta H^\circ(p^\circ) + \int_{p^\circ}^p \Delta V dp$$

$$T_{\text{ad.flame}} = T_i - \frac{\Delta H(T_i)}{C_p(\text{products})} \quad (\text{const. } C_p(\text{products}))$$