

Quiz#2

Feb. 16 (W)

**Student's tutorial from 7-9pm Mondays
and Tuesdays in NH246**

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Helping hrs at PS-3026: Monday 3-5 pm; Wd 3-5 pm

Quantized Energy and Photons

Three phenomena which caused development of quantum theory: black body radiation, photo-electronic effect, and emission spectra



Black-body radiation: red-hot objects are cooler than white-hot

• **Planck: energy can only be absorbed or released from atoms in certain amounts called quanta.**

The relationship between energy and frequency is

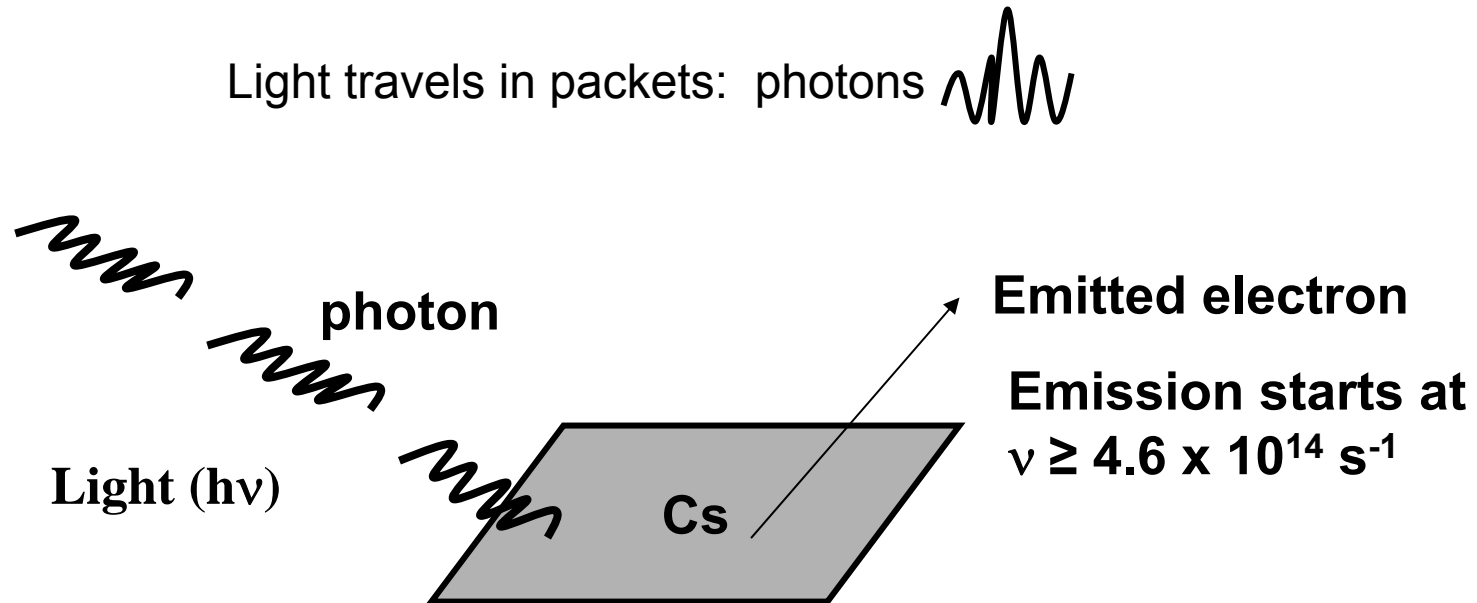
$$E = h\nu$$

Matter can emit or absorb energy only in $N \times h\nu$, where N is whole number

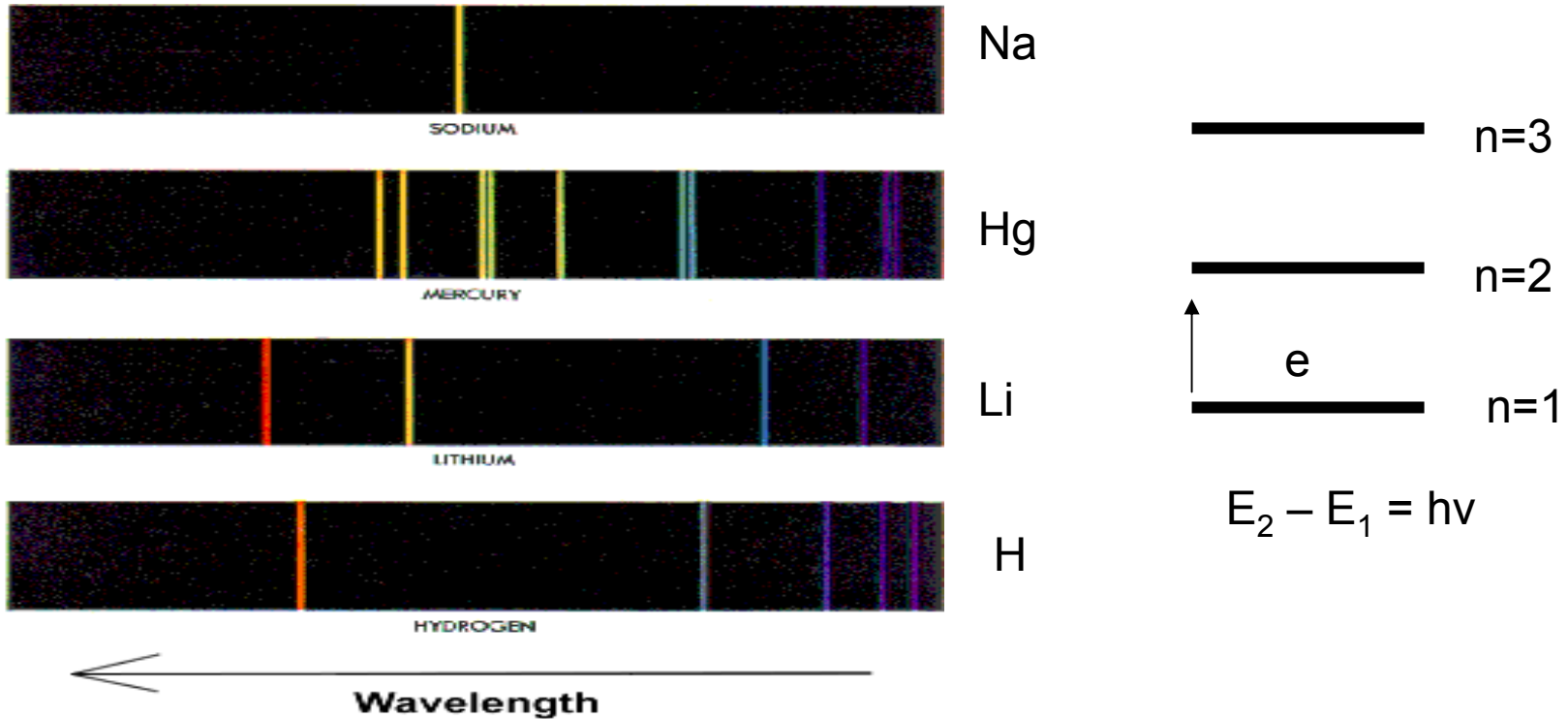
where h is **Planck's constant** (6.626×10^{-34} Jxs).

The Photoelectric Effect and Photons (Einstein's Noble prize)

- light hits the surface of a light metal (Cs): electrons are ejected but only at certain frequencies.
- A photon transfers its energy to an electron. At sufficient amount of energy, an electron can escape the metal surface.



Line Spectra of Atoms (radiation of only specific wavelengths)

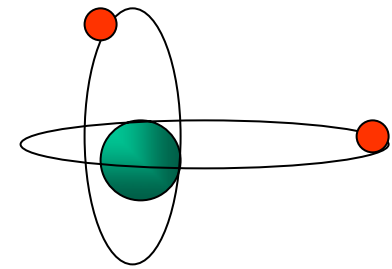


Light hits an atom: atom absorbs certain frequencies (excited state)

atom in excited state emits light at certain frequencies

It is in contrast to continuous spectrum: rainbow

Bohr Model



- The first orbit in the Bohr model has $n = 1$, is closest to the nucleus, and has negative energy by convention.
- The furthest orbit in the Bohr model has n close to infinity and corresponds to zero energy.
- Electrons in the Bohr model can only move between orbits by absorbing and emitting energy in quanta ($h\nu$).
- The amount of energy absorbed or emitted on movement between states is given by

$$\Delta E = E_f - E_i = h\nu$$

Dual nature of electron : wave + particle

Louis de Broglie (1924)

Small particles of matter exhibit wave-like properties

$$E = mc^2$$

$$E = h\nu$$

$$c = \nu\lambda$$

$$mc^2 = h\nu$$

$$\frac{h\nu}{c} = mc = p$$

$$\frac{h\nu}{\nu\lambda} = p$$

$$\frac{h}{\lambda} = p$$

$$\lambda = \frac{h}{p} = \frac{h}{mu}$$

De Broglie wave

What is the de Broglie wavelength (m) of a 60.0 kg athlete running at a speed of 10 m/s ?

$$\lambda = \frac{h}{p} = \frac{h}{mu}$$

$$h = 6.626 \times 10^{-34} \text{ J s}$$

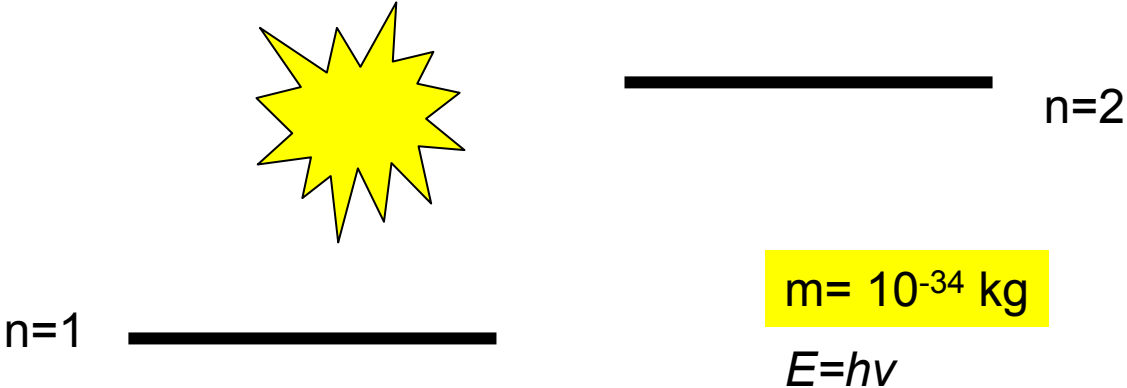
$$\text{J} = \text{kg m}^2 \text{ s}^{-2}$$

$$\lambda = \frac{h}{mu} = \frac{6.626 \times 10^{-34} \frac{\text{kg} \times \text{m}^2}{\text{s}^2} \times \text{s}}{60 \text{ kg} \times 10 \frac{\text{m}}{\text{s}}} = 0.01104 \times 10^{-34} \text{ m}$$

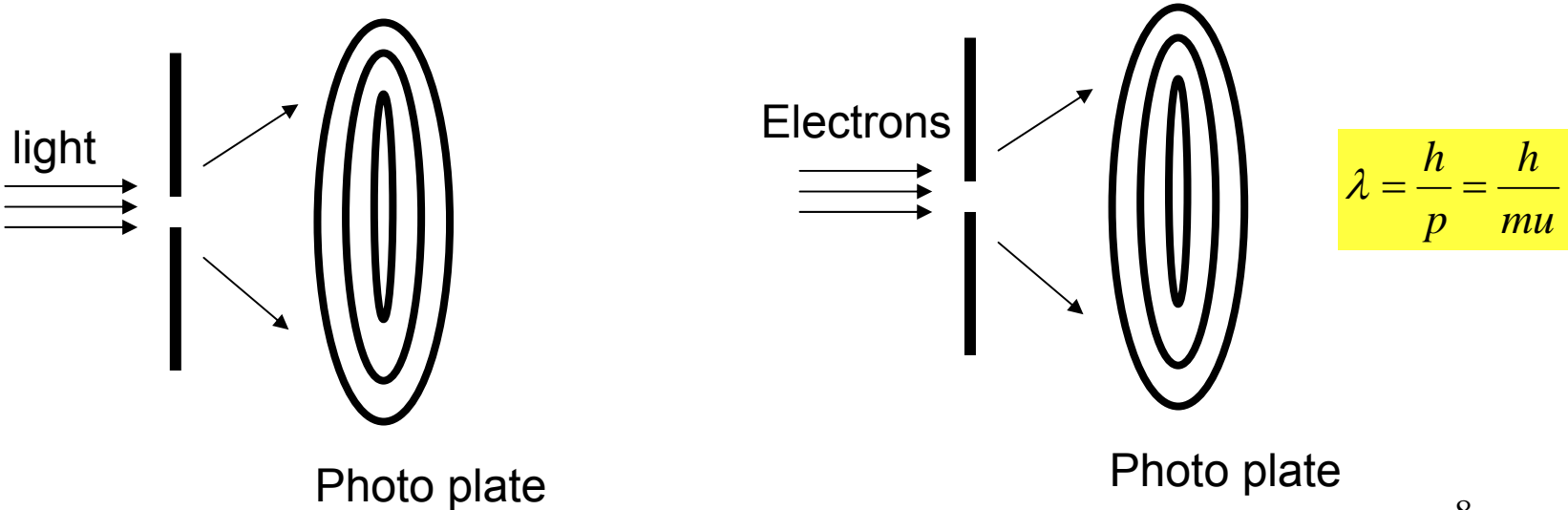
$$= 1.104 \times 10^{-36} \text{ m}$$

Gamma rays: 10^{-11} m

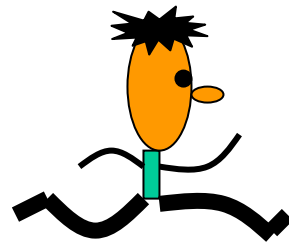
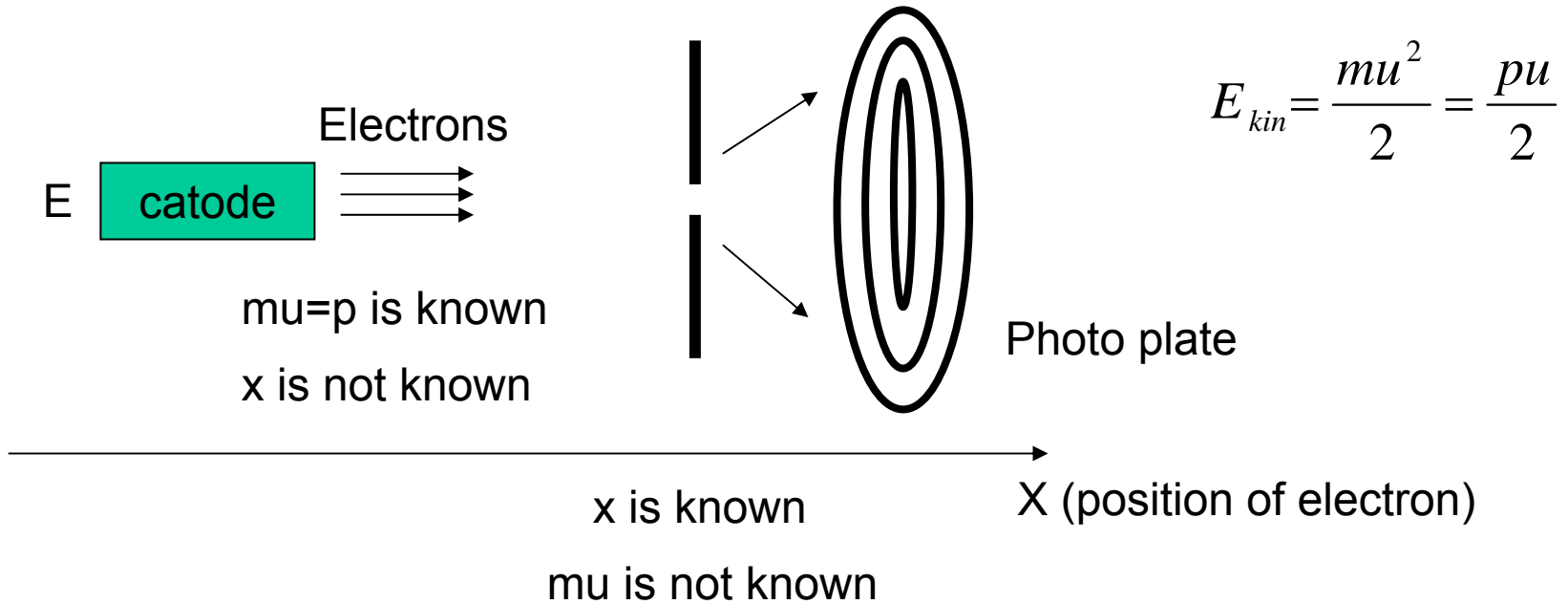
Electron acts as a particle:



Electron acts as a wave:



Heisenberg uncertainty principle



0.0m

100.0m

The *process* of measurement of \bar{e} position changes the energy of the \bar{e}

We cannot know exact position and exact momentum of an electron at the same time

$$\Delta x \times \Delta p \approx h$$

In quantum mechanics, a particle does not have well-defined position and velocity

Heisenberg uncertainty principle

A particle (electron) CAN BE represent by WAVE FUNCTION (Ψ)

Ψ is a number at each point of space that will give the probability of finding the particle at this position.

Schrödinger equation: gives a rate at which Ψ is changing with time

$$ih \frac{\partial}{\partial t} \Psi(\vec{x}, t) = \hat{H} \Psi(\vec{x}, t)$$

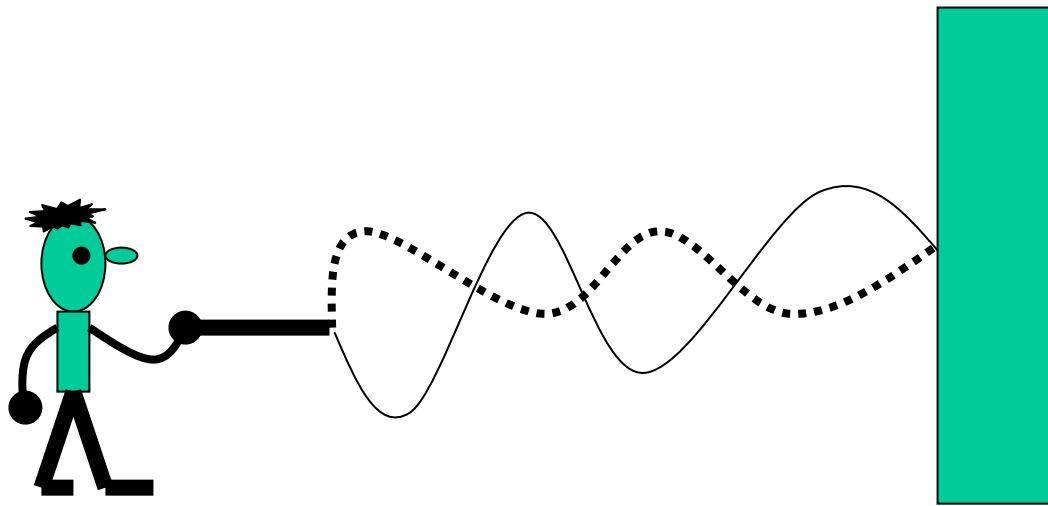
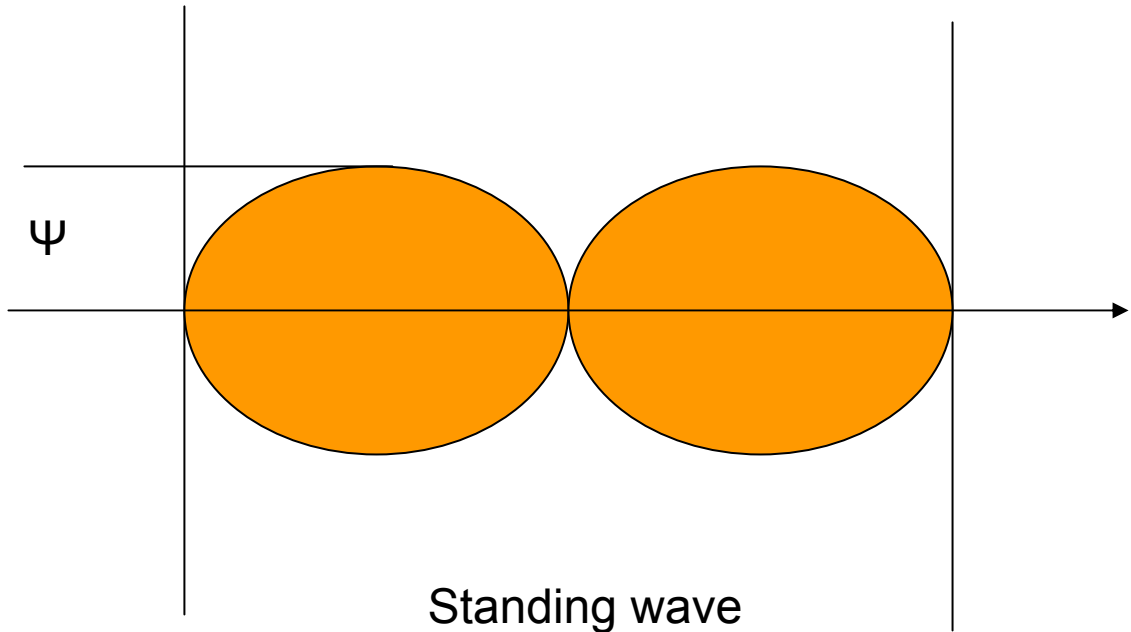
If time is constant

H is energy operator, x is space coordinate, t is time

$$\hat{H} \Psi(\vec{x}) = E \Psi(\vec{x})$$

$$\hat{H} = \hat{T} + \hat{V}$$

T is kinetic energy, V is potential energy



Solution of Sch. Eq. gives the energy of the system and Ψ

Physical meaning of Ψ , postulated by **Born**

Ψ^2 gives a probability of finding electron in elementary volume of space

Quantum mechanics is a theory of probabilities, the values, predicted with Q.M. are average values

Solving Schr. Eq:

Solution gives Ψ for each electron in atom which we called **orbitals**

Each orbital has **energy**

Each orbital has properties described by **quantum numbers**

Ψ and Ψ^2 have approximately the same shape- shape of an orbital

Quantum numbers

Principle q. n. $n = 1, 2, 3, \dots$

Orbital angular momentum $\ell = 0, 1, 2, 3, \dots, (n-1)$

Magnetic quantum number $m_l = -\ell, -\ell+1, \dots, 0, \dots, +\ell$

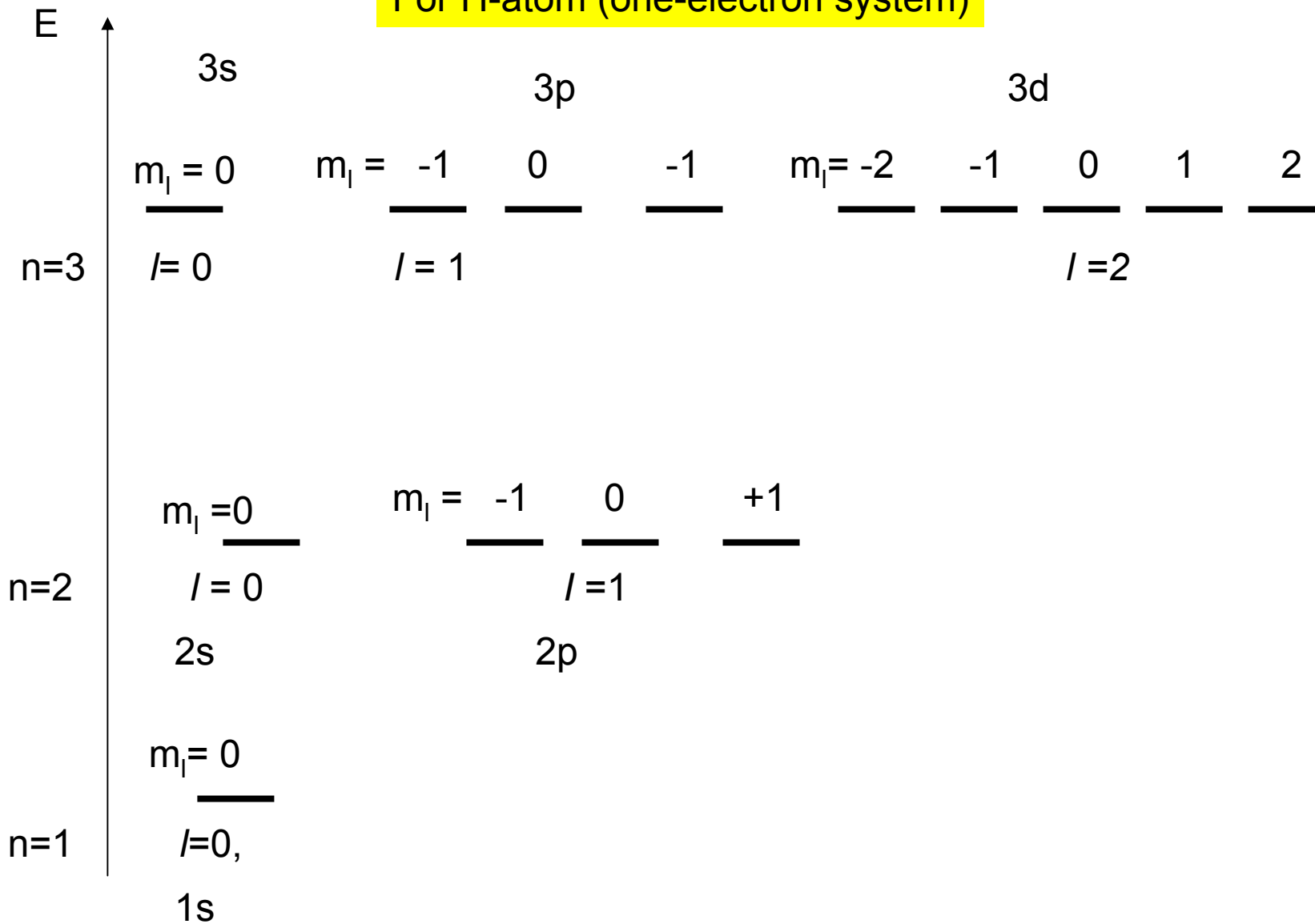
Electronic shells

All orbitals with the same n - principle electronic shell

All orbitals with the same n and ℓ - subshell

$\ell = 0$	1	2	3	4	5
s-subsh	p-subsh	d-subsh	f-subsh	g-subsh	h-subsh

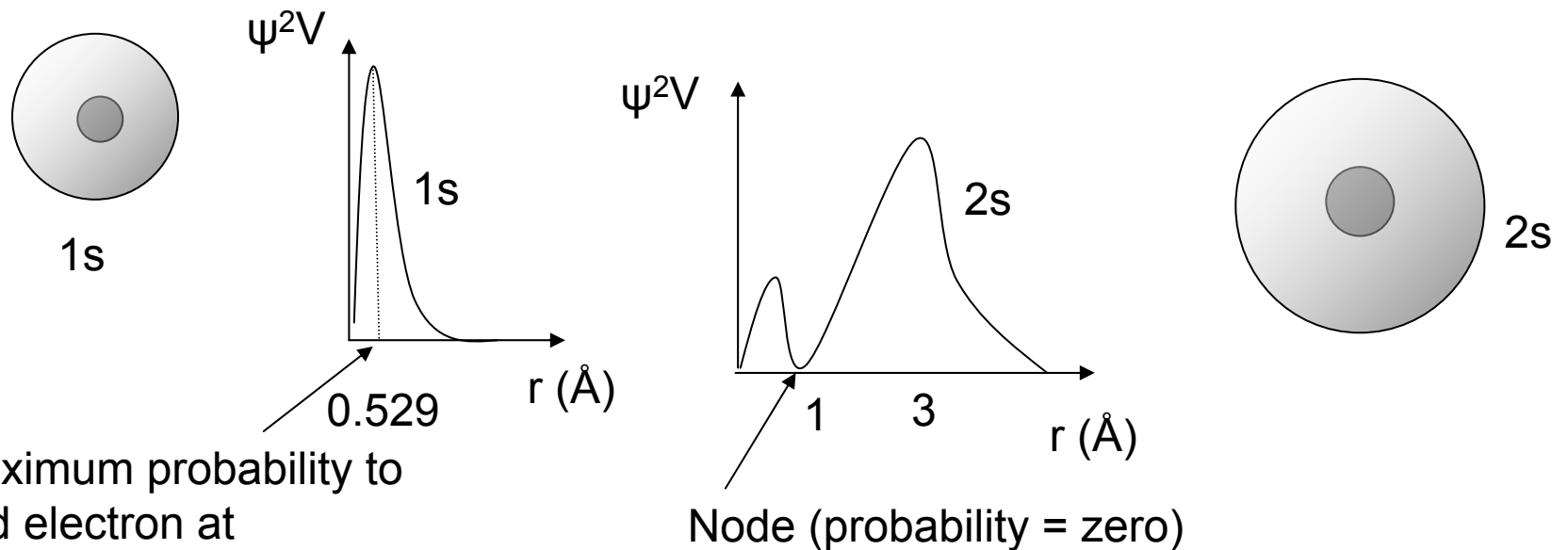
For H-atom (one-electron system)



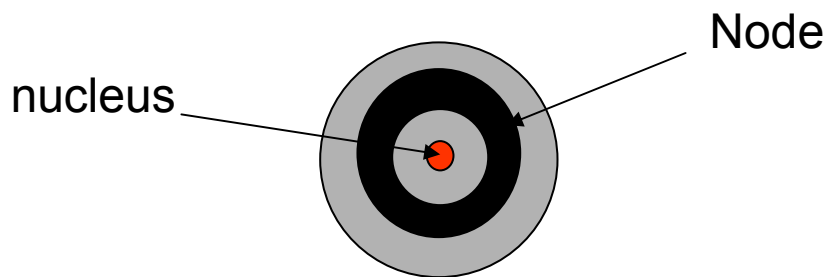
Ψ^2 – gives the probability of finding electron at the certain point in space, i.e.
the probability density

$\Psi^2 \times \text{Volume} = \text{probability of finding electron in that volume} - \text{all the space around atom}$

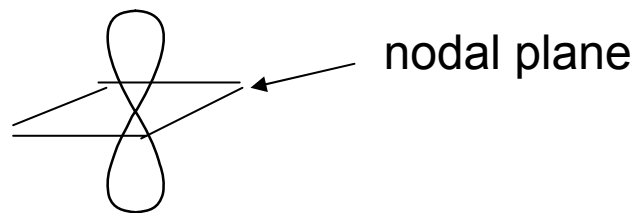
Orbital (solution of Schr. Eq.) – is the probability of finding electron in the space around the nucleus



Section of 2s:



For $l = 1$



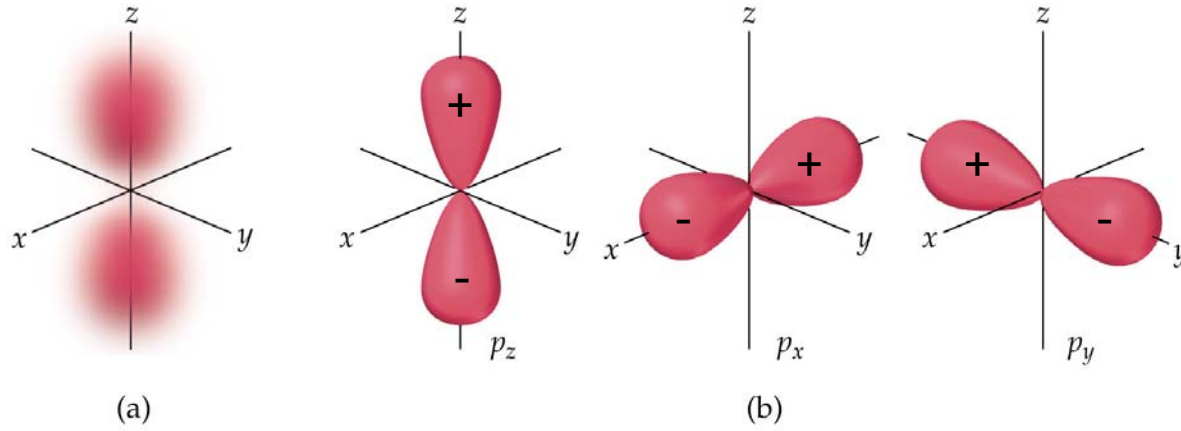
2p

Ψ has the same shape as Ψ^2 but it has a sign (opposite phase)



ℓ gives shapes of orbitals

$m_\ell =$ gives the orientation of atomic orbitals in Cartesian coordinates



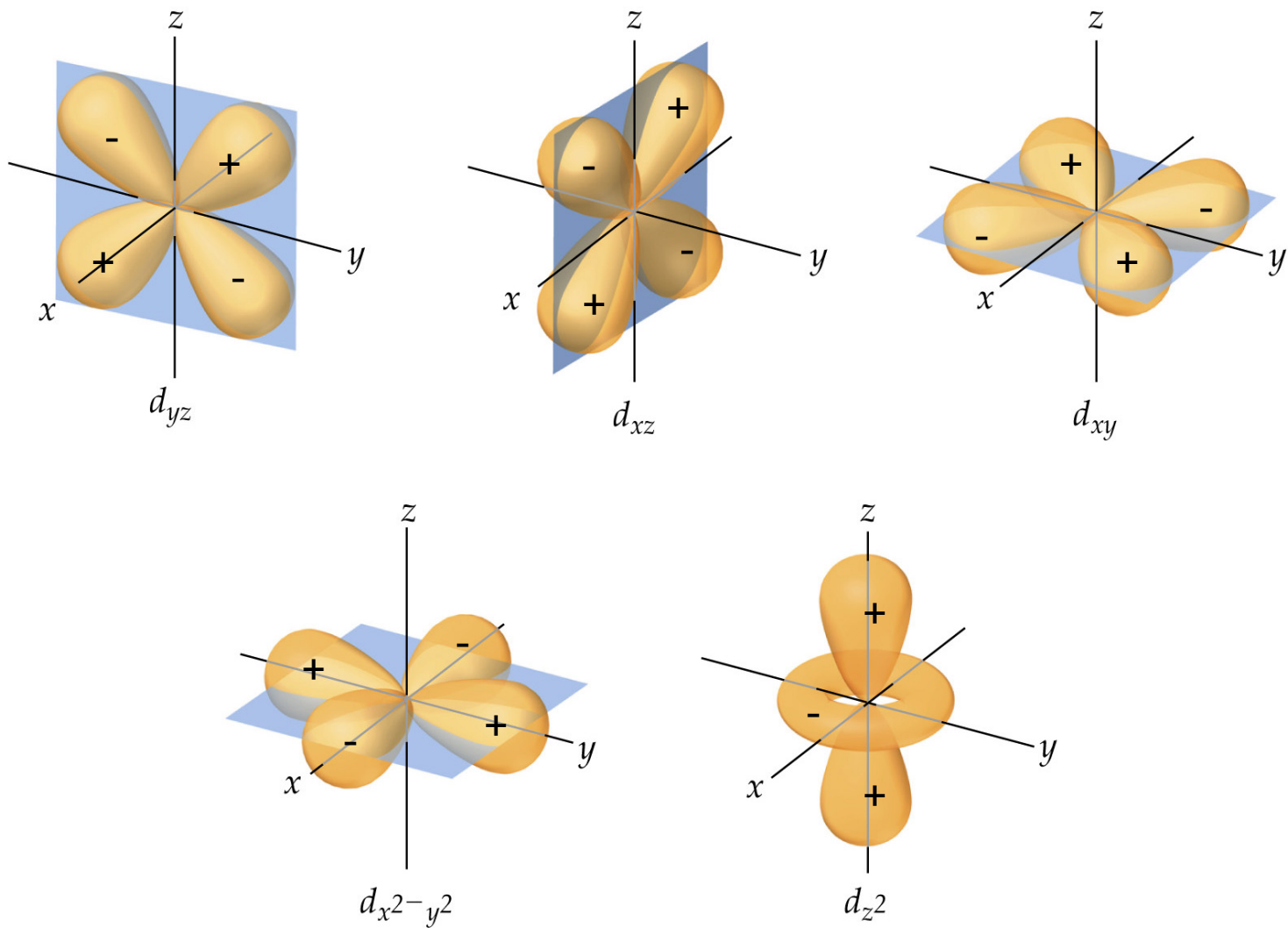
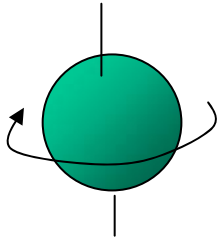


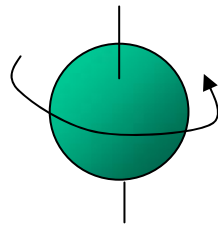
Figure 6.24 in the text

Magnetic spin number: m_s

$m_s = +1/2; -1/2$



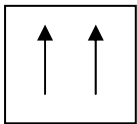
Spin UP and spin DOWN



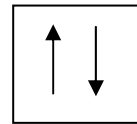
Building the electronic configurations for atoms

Pauli Exclusion Principle:

Two electrons in an atom cannot have the same set of quantum numbers (n , l , m_l , and m_s). Two electrons on the same orbital (n, l, m are the same) must have opposite spins.



~~$n=1, l=0, m_l=0, m_s=1/2$~~



$n=1, l=0, m_l=0, m_s = 1/2$

$n=1, l=0, m_l=0, m_s = -1/2$