Bond dipoles, molecular dipoles, quadrupoles

Bond dipole- local momentum associated with polar covalent bond


$$
\text { 1D= } 0.39 \text { au (atomic unit) }
$$

au: unit of mass- electron mass, unit of charge- proton charge, unit of angular momentum- $\hbar$

Molecular dipole moments- watch for symmetry!


Compare $\mu$ (D)




## Quadrupole, octupole,.. (multipoles)

## Multipoles- interaction of arrays of point charges

n -pole- an array of n point charges with an n-pole moment but NO lower moments

Monopole: point charge, monopole moment- the overall charge
Dipole- array of two point charges with no net charge (no monopole moment)

Quadrupole: array of 4 charges, no dipole moment, no net charge


Octupole- 8 point charges, no quadrupole


For inter-molecular forces:
The interaction falls off more rapidly with higher order of $n$-poles

Dipole-dipole interaction: $\mathrm{r}^{-3}$ (usually about $2 \mathrm{~kJ} / \mathrm{mol}$ )
$2^{n}$-pole with $2^{m}$ pole: $1 /\left(n^{n+m-1}\right)$
Quadrupole-quadrupole: $1 / r^{4+4-1}=r^{-7}$
n-poles and molecular orbitals


Standard bond angles are know for organic systems. Standard bond lengths?
Typical bond lengths, in $\AA \AA$, for some covalent bonds:
Single bonds:

| $\mathrm{C}\left(\mathrm{sp}^{3}\right)-\mathrm{C}\left(\mathrm{sp}^{3}\right)$ |  | 1.53-1.55 | Double bonds |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}\left(\mathrm{sp}^{3}-\mathrm{C}\left(\mathrm{sp}^{2}\right)\right.$ |  | $\begin{aligned} & 1.53-1.55 \\ & 1.49-1.52 \end{aligned}$ | $\mathrm{C}\left(\mathrm{sp}^{2}\right)$-C(sp ${ }^{2}$ ) | alkenes | 1.31-1.34 |
| $\mathrm{C}\left(\mathrm{sp}^{2}\right)$ - $\mathrm{C}\left(\mathrm{sp}^{2}\right)$ |  | 1.49-1.52 | $\mathrm{C}\left(\mathrm{sp}^{2}\right)$-C(sp ${ }^{2}$ ) | arenes | 1.38-1.40 |
|  |  |  | $\mathrm{C}\left(\mathrm{sp}^{2}\right)-\mathrm{O}\left(\mathrm{sp}^{2}\right)$ | aldehydes and |  |
| conjugated |  | 1.45-1.46 |  | ketones | 1.19-1.22 |
| nonc | gated | 1.47-1.48 | $\mathrm{C}\left(\mathrm{sp}^{2}\right) \mathrm{O}\left(\mathrm{sp}^{2}\right)$ | esters | 1.19-1.20 |
| C(sp)-C(sp) |  | 1.37-1.38 |  | amides |  |
| $\mathrm{C}\left(\mathrm{sp}^{3}\right)$ - ${ }^{\left(s p p^{3}\right)}$ | ethers | 1.42-1.44 | $\mathrm{C}\left(\mathbf{s p}^{2}\right)-\mathrm{O}\left(\mathrm{sp}^{2}\right)$ | amides | $\begin{aligned} & 1.225-1.24 \\ & 135 \end{aligned}$ |
| $\mathrm{C}\left(\mathrm{sp}^{3}\right)-\mathrm{N}\left(\mathrm{sp}^{3}\right)$ | amines | 1.46-1.48 | C( $\mathbf{s p}^{2}$ )-N(sp ${ }^{2}$ ) | imines | 1.35 |
| C-F |  | 1.39-1.43 | Triple bonds |  |  |
| $\mathrm{C}-\mathrm{Cl}$ |  | 1.78-1.85 | C(sp)-C(sp) | alkynes | 1.17-1.20 |
| $\mathrm{C}-\mathrm{Br}$ |  | 1.95-1.98 |  |  |  |
| C-I |  | 2.15-2.18 |  |  |  |
| C( sp $^{3}$ )-H |  | 1.09-1.10 |  |  |  |
| $\mathrm{C}\left(\mathrm{sp}^{2}\right)-\mathrm{H}$ |  | 1.075-1.0 |  |  |  |
| C(sp)-H |  | 1.06 |  |  |  |
| $\mathrm{N}-\mathrm{H}$ |  | 1.00-1.02 |  |  |  |
| O-H |  | 0.96-0.97 |  |  |  |

Covalent, Ionic, and van der Waals radii (in $\AA$ ) of Selected Atoms

| Atom | Covalent | vdW | ion | lonic |
| :--- | :--- | :--- | :--- | :--- |
| C | 0.77 | 1.68 | - | - |
| H | 0.30 | 1.11 | $\mathrm{H}^{-}$ | 2.08 |
| N | 0.70 | 1.53 | - | - |
| O | 0.66 | 1.50 | - | - |
| F | 0.64 | 1.51 | $\mathrm{~F}^{-}$ | 1.36 |
| Cl | 0.99 | 1.84 | $\mathrm{Cl}^{-}$ | 1.81 |
| Br | 1.14 | 1.96 | Br | 1.95 |
| I | 1.33 | 2.13 | F | 2.16 |

Polarizability: the ability of the electron cloud to distort in response to an external electric field

As a result, the induced dipole appears in addition to permanent dipole (if present)

> Polarizability= magnitude of the dipole induced by one unit of field gradient (in units of volume, $\mathrm{cm}^{3}$ )

Atomic polarizabilities ( $\alpha, \AA^{3}=\mathrm{cm}^{3} \times 10^{-24}$ )

| 0.6668 |  |  |  |  |  | $H e$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| C | 1.76 | N | 1.10 | O | 0.802 | F | 0.557 |
|  |  | P | 3.13 | S | 2.90 | CI | 2.18 |
|  |  |  |  |  |  | Br | 3.05 |
|  |  |  |  |  |  | I | $\approx 5.0$ |

Selected molecular polarizabilities

| $\mathrm{CH}_{4}$ | 2.6 | $\mathrm{NH}_{3}$ | 2.21 | $\mathrm{H}_{2} \mathrm{O}$ | 1.45 | $\mathrm{H}_{2} \mathrm{~S}$ | 3.8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CO}_{2}$ | 2.91 | $\mathrm{CS}_{2}$ | 8.8 | $\mathrm{CF}_{4}$ | 3.84 | $\mathrm{CCl}_{4}$ | 11.2 |
| $\mathrm{C}_{2} \mathrm{H}_{2}$ | 3.6 | $\mathrm{C}_{2} \mathrm{H}_{4}$ | 4.25 | $\mathrm{C}_{2} \mathrm{H}_{6}$ | 4.45 | $\mathrm{CH}_{3} \mathrm{OH}$ | 3.23 |
| Benzene | 10.32 | Cyc | ene | 10.7 | Cyc | ane | 11.0 |

## Symmetry of molecular systems

Symmetry elements: plane, axis and point (center of inversion)

## Symmetry operations:

1. rotation about a proper axis. For example, $\mathbf{C}_{2}$ means rotation about 360\%/2 (180 $)$, $\mathrm{C}_{3}$ - rotation about $360^{\circ} / 3\left(120^{\circ}\right)$, where n is an order of the axis.
2. reflection in a plane of symmetry, $\boldsymbol{\sigma}$. there are 3 types of planes. $\boldsymbol{\sigma}_{\mathrm{h}}$ is perpendicular to $\boldsymbol{C}_{\mathrm{n}}$ (main axis); $\boldsymbol{\sigma}_{\mathrm{v}}$ contains the main axis, $\boldsymbol{\sigma}_{\mathrm{d}}$ divides in half the angle between the two $\mathbf{C}_{2}$ which are perpendicular to $\mathbf{C}_{\mathbf{n}}$.
3. inversion of all atoms through a center of symmetry, (center of inversion) denoted as $i . \mathrm{C}_{2} \times \boldsymbol{\sigma}_{\mathrm{h}}=\mathbf{i}$
4. identity operation E - position of atoms do not changecorresponds to the rotation about $360^{\circ}$.

All other operations is just a combination of the symmetry operations described above.

Of particular importance is rotation about an axis, $\mathbf{C}_{\mathrm{n}}$, followed by reflection through the plane perpendicular to the axis, $\boldsymbol{\sigma}_{\mathrm{h}}$. This operation is called a rotation about an improper axis, denoted as $\mathbf{S}_{\mathrm{n}}$.

A necessary and sufficient criterion for chirality is an absence of $S_{n}$ axes. If any $\mathrm{S}_{\mathrm{n}}$ exists the structure is achiral

$$
\text { Symmetry elements of } \mathrm{H}_{2} \mathrm{O}
$$



Identity operation


$\mathrm{H}_{2} \mathrm{O}$ has 4 elements of symmetry: $\mathrm{E}_{1} \mathrm{C}_{2}$, and $2 \sigma_{v}$ This set of elements is called a $\mathrm{C}_{2 \mathrm{~V}}$ symmetry group

Symmetry elements of $\mathrm{NH}_{3}$ :


Trigonal pyramidal

Rotation about $120^{\circ}$


$\mathrm{NH}_{3}$ has 5 elements of symmetry: $\mathrm{E}, \mathrm{C}_{3}$, and $3 \sigma_{v}$ This set of elements is called a $\mathrm{C}_{3 v}$ symmetry group.

Symmetry groups:
No axis other than $\mathrm{C}_{1}: \mathrm{C}_{1}$ (no symmetry), $\mathrm{C}_{\mathrm{s}}, \mathrm{C}_{\mathrm{i}}$



2. Only one axis with $n>1: C_{n}, S_{n}, C_{n v}, C_{n h}$

dihedral groups, D : contain $\mathrm{C}_{\mathrm{n}}$ and $\mathrm{n}_{2}$ perpendicular to $\mathrm{C}_{\mathrm{n}}$. $D_{n}, D_{n h}, D_{n d}$

$\mathrm{D}_{2 \mathrm{~d}}$

The cubic groups: $\mathrm{Td}\left(\mathrm{E}, 8 \mathrm{C}_{3}, 3 \mathrm{C}_{2}, 6 \mathrm{~S}_{4}, 6 \sigma_{\mathrm{d}}\right)$, Oh


